

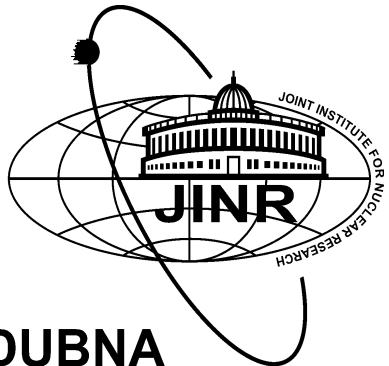
GBU approach to quark-hadron matter

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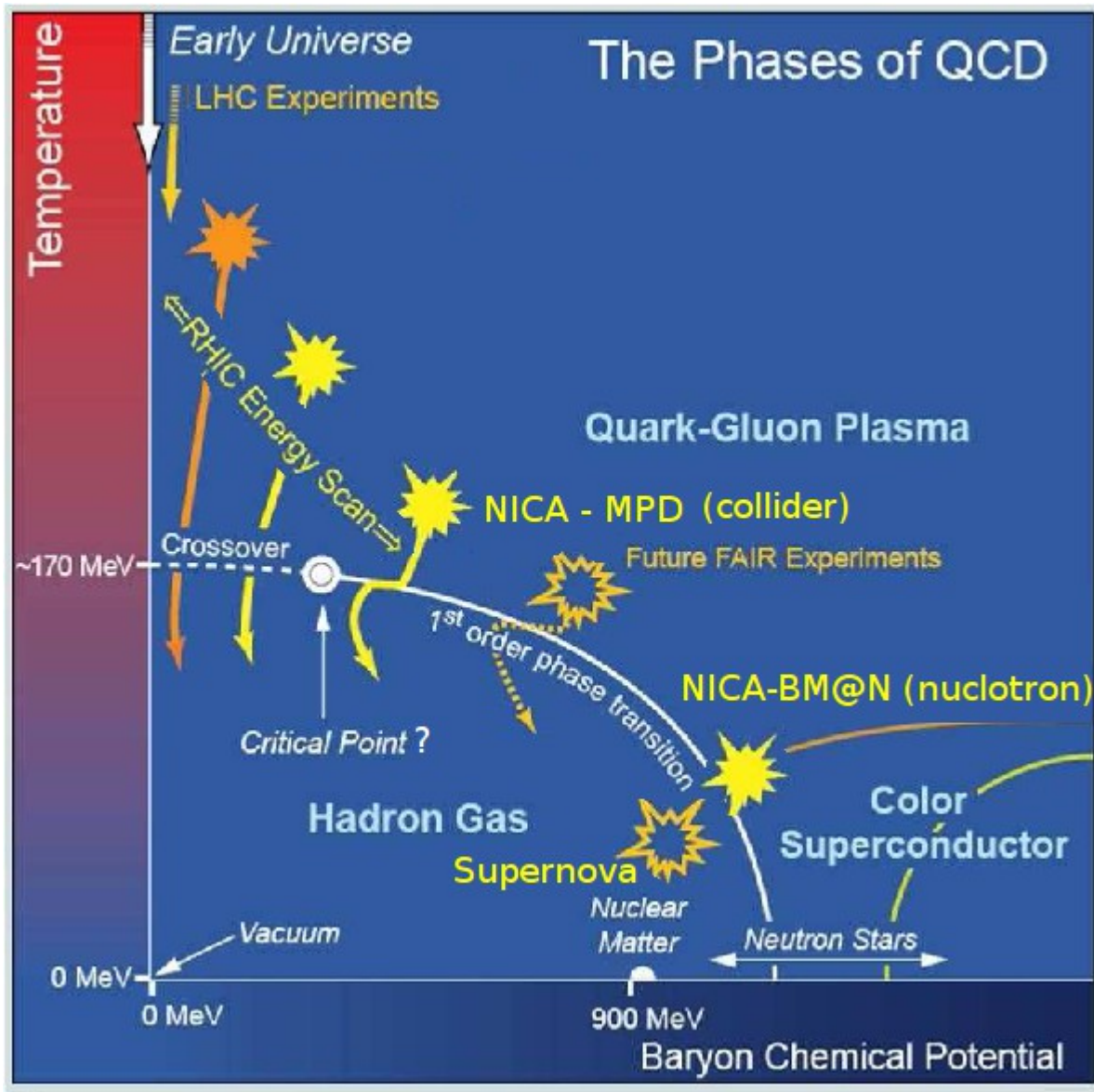
University of Wroclaw, Poland & JINR Dubna & MEPhI Moscow, Russia

- 1. Introduction: Beth-Uhlenbeck (BU) and Generalized BU**
- 2. GBU from Φ -derivable approach: 2-loop approximation**
- 3. GBU EoS for quark-hadron matter in (P)NJL-type models**

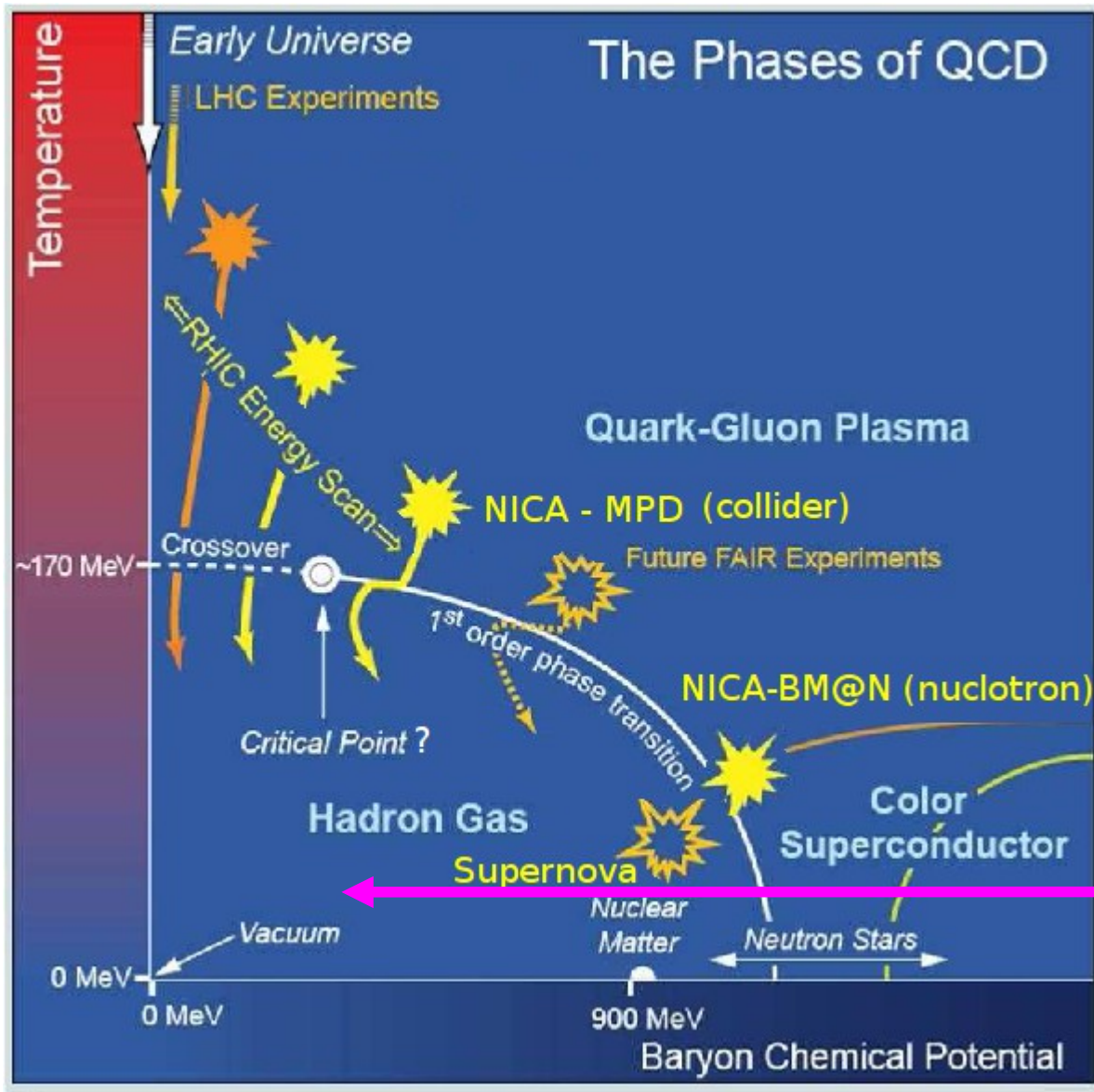
CA15213 “THOR” WG Meeting, FIAS Frankfurt, 19. January 2017



The Goal: Theory of the QCD Phase Diagram



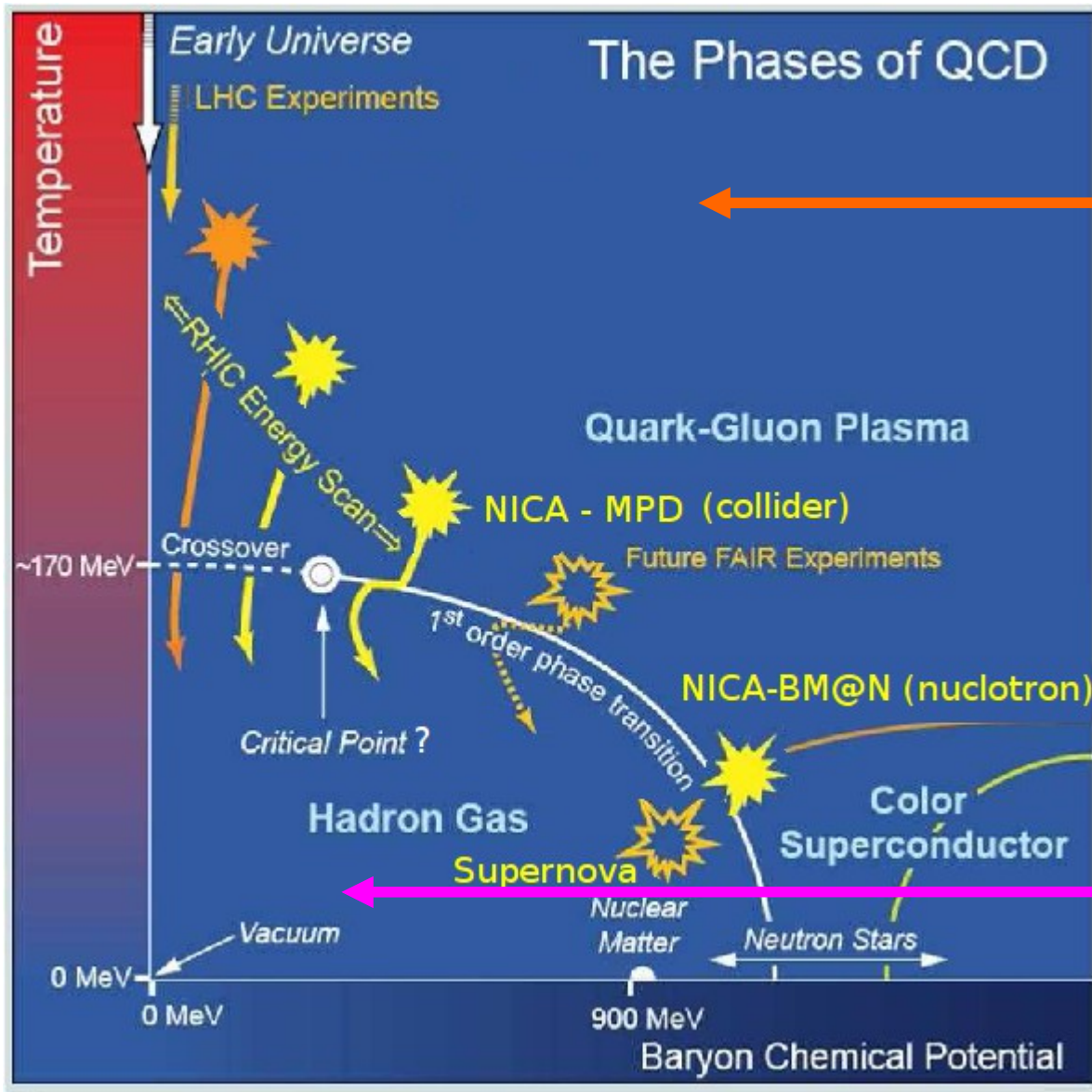
The Goal: Theory of the QCD Phase Diagram



Statistical Model of
Hadron Resonance Gas

Well established for
Description of chemical
freezeout

The Goal: Theory of the QCD Phase Diagram



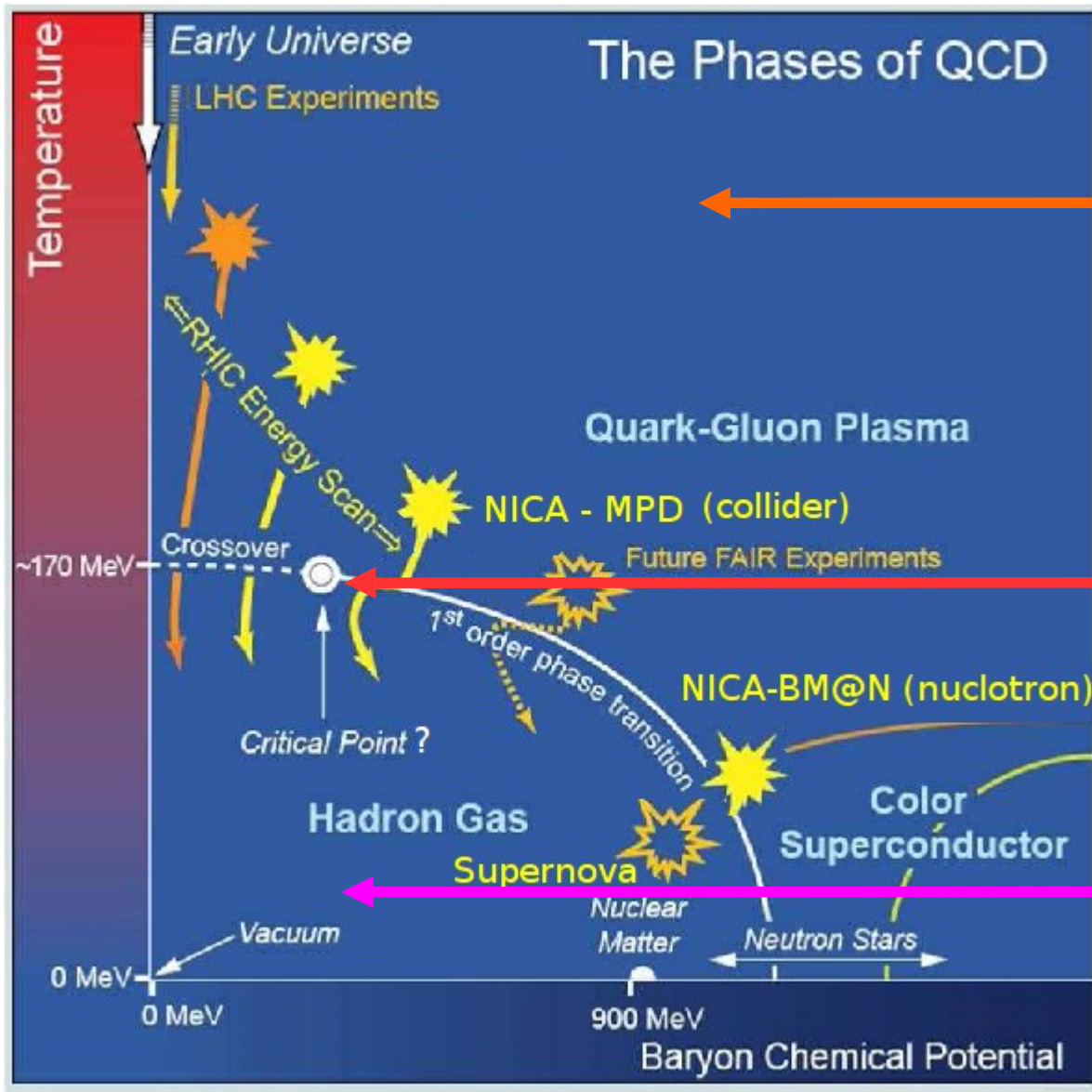
Perturbative QCD

Approximately selfconsistent
HTL resummation
($T > 2.5 T_c$, $\mu > 1500$ MeV)

Statistical Model of Hadron Resonance Gas

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The Goal: Theory of the QCD Phase Diagram



Perturbative QCD

Approximately selfconsistent HTL resummation
($T > 2.5 T_c$, $\mu > 1500$ MeV)

QCD Phase transition(s)

Mott dissociation of hadrons,
Deconfinement, χ SR

Statistical Model of Hadron Resonance Gas

Well established for
Description of chemical
freezeout

Introduction: Beth-Uhlenbeck vs. Generalized BU

Beth-Uhlenbeck: 2nd virial coefficient B(T)

$$pV = NkT \left(1 + \frac{B(T)}{V} + \frac{C(T)}{V^2} + \dots \right)$$

BU for virial expansion of density:

$$n(\mu, T) = n_{\text{free}}(\mu, T) + 2n_{\text{corr}}(\mu, T)$$

$$n_{\text{free}}(\mu, T) = 4 \int \frac{d^3p}{h^3} e^{-(p^2/2m - \mu)/T} = \frac{4}{\lambda^3} e^{\mu/T}$$

$$n_{\text{corr}}(\mu, T) = \int \frac{d^3\mathbf{P}}{h^3} e^{-(P^2/4m - 2\mu)/T} \int_{-\infty}^{\infty} \frac{dE}{\pi} e^{-E/T} D(E)$$

$$= \frac{2^{3/2}}{\lambda^3} e^{2\mu/T} \int_{-\infty}^{\infty} \frac{dE}{\pi} e^{-E/T} D(E).$$

Density of states: bound and scattering part

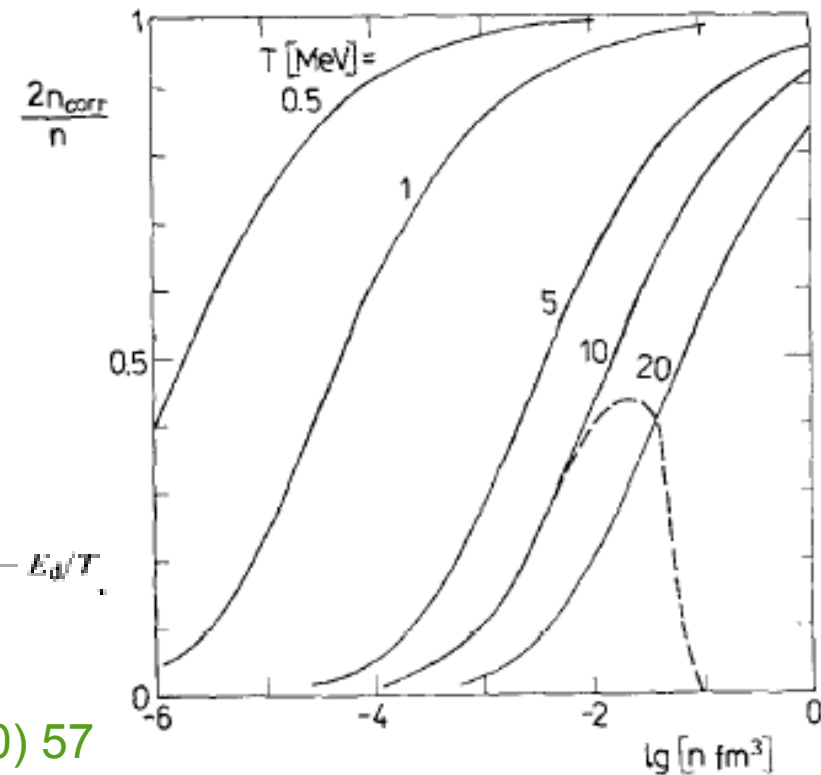
$$D(E) = \sum_x c_x \left[\pi \delta(E - E_x) + \frac{d}{dE} \delta_x(E) \right],$$

Example: Deuterons in nuclear matter

$$n = n_{\text{free}} + 2n_{\text{free}}^2 I(T)$$

$$I(T) = \lambda^3 \frac{2^{1/2}}{8} \left[3(e^{-E_d/T} - 1) + \int_0^{\infty} \frac{dE}{\pi T} e^{-E/T} \sum_x c_x \delta_x(E) \right].$$

For $T \ll E_d$: $n = n_{\text{free}} + 2n_{\text{deut}}$, $n_{\text{deut}} = n_{\text{free}}^2 \lambda^3 3 \frac{2^{1/2}}{8} e^{-E_d/T}$.



Introduction: Beth-Uhlenbeck vs. Generalized BU

Thermodynamic Greens function approach:

$$n(1, \mu_1, T) = \int \frac{dE}{2\pi} f_1(E) A(1, E)$$

$$A(1, E) = \frac{2\Sigma_1(1, E - i0)}{(E - E(1) - \Sigma_R(1, E))^2 + \Sigma_I(1, E - i0)^2} = \frac{2\pi \delta(E - e(1))}{1 - ((d/dz) \Sigma_R(1, z))|_{z=e(1)+i0}} - 2\Sigma_1(1, E + i0) \frac{d}{dE} \frac{\mathbf{P}}{E - e(1)}$$

Density formula
(free and corr. Quasiparticles):

$$n(\mu, T) = n_{\text{free}}(\mu, T) + 2n_{\text{corr}}(\mu, T),$$

$$\Sigma(1, z_\nu) = T \sum_2 \sum_{z_\nu'} [T(1212, z_\nu + z_\nu') - \text{ex}] G(2, z_\nu')$$

$$n_{\text{corr}}(\mu, T) = \int \frac{dE}{2\pi} g(E) F(E)$$

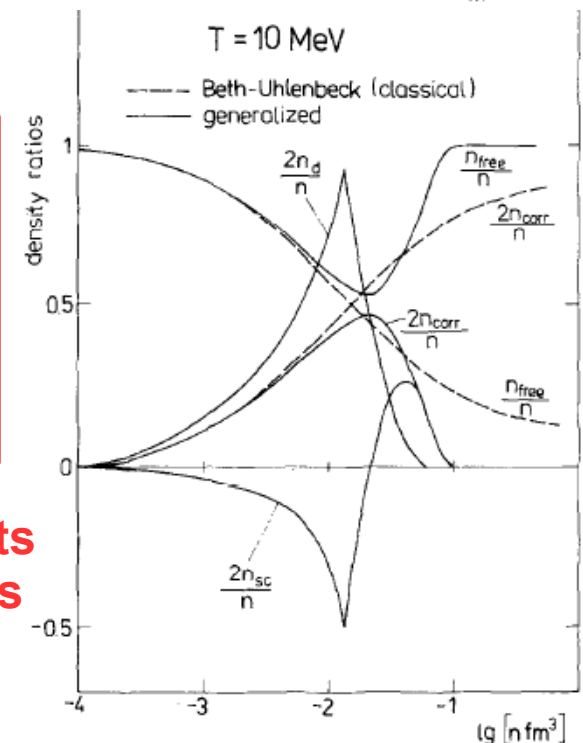
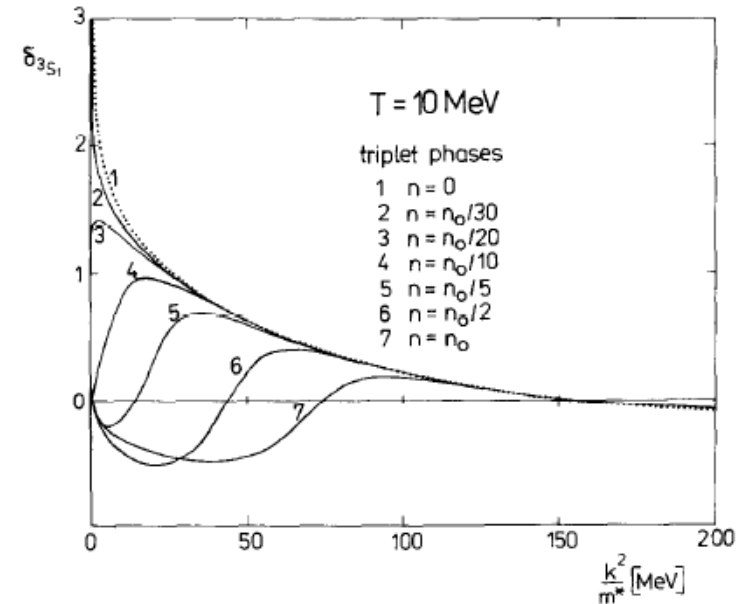
$$F(E) = F_{\text{deut}}(E) + \frac{2}{4\pi} \sum_x c_x F_x(E),$$

$$F_{\text{deut}}(E) = 6 \sum_{\mathbf{K} > \mathbf{K}^{\text{Mott}}} \pi \delta(E - E_b(\mathbf{K}, \mu, T)).$$

$$F(E) = \sum_{12} [1 - f(e(1)) - f(e(2))] \cdot \left[(T_1(1212, E + i0) - \text{ex}) \frac{d}{dE} \frac{\mathbf{P}}{e(1) + e(2) - E} - \pi \delta(E - e(1) - e(2)) \frac{d}{dE} (T_R(1212, E + i0) - \text{ex}) \right]$$

$$F_x(E) = 8\pi \sum_{\mathbf{K}} \sin^2 \delta_x(E, \mathbf{K}, \mu, T) \frac{d}{dE} \delta_x(E, \mathbf{K}, \mu, T).$$

The $\sin^2 \delta$ term accounts for quasiparticle effects



Φ -derivable approach, 2-loop approximation

J.-P. Blaizot, E. Iancu, A. Rebhan, Phys. Rev. D 63 (2001) 065003

Skeleton expansion for thermodynamic potential and entropy

$$\beta\Omega[D] = -\log Z = \frac{1}{2} \text{Tr} \log D^{-1} - \frac{1}{2} \text{Tr} \Pi D + \Phi[D]$$

↑
Inv. Temp: 1/T

↑
trace in conf. Space

↑
self-energy related to D

$$-\Phi[D] = \frac{1}{12} \text{Tr} \left(\text{circle with horizontal line} \right) + \frac{1}{8} \text{Tr} \left(\text{two circles} \right) + \frac{1}{48} \text{Tr} \left(\text{circle with two horizontal lines} \right) + \dots$$

Dyson equation:

$$D^{-1} = D_0^{-1} + \Pi$$

Free propagator D_0 is known

Essential property of $\Omega[D]$ is Stationarity under variation of D: $\delta \Omega[D] / \delta D = 0$

This implies $\delta \Phi[D] / \delta D = 1/2 \Pi$

Physical propagator and selfenergy are defined self-consistently !

Self-consistent approximations are defined by the **choice of Φ**

→ Φ – derivable theories

G. Baym, Phys. Rev. 127 (1962) 1391; Vanderheyden & Baym; J. Stat. Phys. 93, 843 (1998)

Approximately selfconsistent thermodynamics

Matsubara summation:

$$\Omega/V = \int \frac{d^4k}{(2\pi)^4} n(\omega) [\text{Im} \log(-\omega^2 + k^2 + \Pi) - \text{Im} \Pi D] + T\Phi[D]/V$$

Analytic properties:

$$D(\omega, k) = \int_{-\infty}^{\infty} \frac{dk_0}{2\pi} \frac{\rho(k_0, k)}{k_0 - \omega}, \quad \text{Im} D(\omega, k) \equiv \text{Im} D(\omega + i\epsilon, k) = \frac{\rho(\omega, k)}{2}.$$

Thermodynamics from entropy density: $S = -\partial(\Omega/V)/\partial T$.

$$S = - \int \frac{d^4k}{(2\pi)^4} \frac{\partial n(\omega)}{\partial T} \text{Im} \log D^{-1}(\omega, k) + \int \frac{d^4k}{(2\pi)^4} \frac{\partial n(\omega)}{\partial T} \text{Im} \Pi(\omega, k) \text{Re} D(\omega, k) + S'$$

$$S' \equiv - \left. \frac{\partial(T\Phi/V)}{\partial T} \right|_D + \int \frac{d^4k}{(2\pi)^4} \frac{\partial n(\omega)}{\partial T} \text{Re} \Pi \text{Im} D \longrightarrow 0$$

for two-loop skeleton diagrams

Loosely speaking: S' accounts for residual interactions of “independent quasiparticles”

$$d/d\omega [\text{Im} \log D^{-1} + \text{Im} \Pi \text{Re} D] = 2 \text{Im} [D \text{Im} \Pi (d/d\omega D^*) \text{Im} \Pi] = 2 \sin^2 \delta \, d\delta/d\omega, \text{ for } D = |D|e^{i\delta}$$

D. B., in preparation (2017)

Proof of cancellations resulting in $S'=0$

(I)

$$S' \equiv -\left. \frac{\partial(T\Phi/V)}{\partial T} \right|_D + \int \frac{d^4k}{(2\pi)^4} \left\{ \frac{\partial n(\omega)}{\partial T} \text{Re} \Pi \text{Im} D \right\}$$

First term

$$-\frac{T}{V}\Phi = \frac{g^2}{12}T^2 \sum_{\omega_1, \omega_2} \int \frac{d^3k_1 d^3k_2}{(2\pi)^6} D(\omega_1, |k_1|) D(\omega_2, |k_2|) D(-\omega_1 - \omega_2, |-k_1 - k_2|)$$

Spectral representation

$$D(\omega, k) = \int_{-\infty}^{\infty} \frac{dk_0}{2\pi} \frac{\rho(k_0, k)}{k_0 - \omega}$$

Matsubara sums

$$-\frac{T}{V}\Phi = \frac{g^2}{12}T^2 \sum_{\omega_1, \omega_2} \int \frac{d^4k d^4k' d^4k''}{(2\pi)^9} \delta^{(3)}(\mathbf{k} + \mathbf{k}' + \mathbf{k}'') \rho(k) \rho(k') \rho(k'') \frac{-1}{\omega_1 - k_0} \frac{-1}{\omega_2 - k'_0} \frac{1}{\omega_1 + \omega_2 + k''_0}$$

Partial fraction decomposition of the three energy denominators and Matsubara summation over ω_1, ω_2 yields:

$$\frac{1}{k_0 + k'_0 + k''_0} \{ [n(k''_0) + 1][n(k_0) + n(k'_0) + 1] + n(k_0)n(k'_0) \}$$

Temperature derivative and renaming variables under the integrals

$$\partial_T [n(k_0 + n(k'_0) + n(k''_0) + n(k'_0)n(k_0) + n(k'_0)n(k''_0) + n(k_0)n(k''_0))] \rightarrow 3\partial_T n(k_0) [1 + n(k'_0) + n(k''_0)]$$

Proof of cancellations resulting in $S'=0$

(II)

Second term:

$$\begin{aligned} \text{Re}\Pi(\omega, q) &= -\frac{g^2}{2} \int \frac{d^3k}{(2\pi)^3} \int \frac{dk_0}{2\pi} \int \frac{dk'_0}{2\pi} \rho(k_0, |k|) \rho(k'_0, |\mathbf{k} + \mathbf{q}|) \sum_{\omega_1} \frac{1}{\omega_1 - k_0} \frac{1}{\omega_1 + \omega - k'_0} \\ &= -\frac{g^2}{2} \int \frac{d^3k}{(2\pi)^3} \int \frac{dk_0}{2\pi} \int \frac{dk'_0}{2\pi} \rho(k_0, |k|) \rho(k'_0, |\mathbf{k} + \mathbf{q}|) \frac{1 + n(k_0) + n(k'_0)}{\omega + k_0 + k'_0} \end{aligned} \quad (7)$$

$$\begin{aligned} &\int \frac{d^4q}{(2\pi)^4} \frac{\partial n(k_0)}{\partial T} \text{Re}\Pi(\omega, q) \text{Im}D(\omega, q) = \\ &= -\frac{g^2}{2 \cdot 2} \int \frac{d^4q}{(2\pi)^4} \int \frac{d^k}{(2\pi)^4} \int \frac{d^4k'}{2\pi} \delta^{(3)}(\mathbf{q} + \mathbf{k} + \mathbf{k}') \rho(q) \rho(k) \rho(k') \partial_T n(q_0) [1 + n(k_0) + n(k'_0)] \frac{1}{q_0 + k_0 + k'_0} \end{aligned} \quad (8)$$

This proves the cancellation of S' for the scalar theory with cubic selfinteraction in the 2-loop approximation (sunset diagram) for the Φ - functional.

This cancellation holds as well for the pressure and the density!

For the pressure we obtain

$$p(T) = - \int \frac{d^4q}{(2\pi)^4} n(q_0) [\delta(q) - \sin \delta(q) \cos \delta(q)] = - \int \frac{d^4q}{(2\pi)^4} T \ln \left(1 - e^{-q_0/T} \right) \frac{\partial \delta(q)}{\partial q_0} 2 \sin^2 \delta(q) \quad (9)$$

Note that in the approximation $\delta(q_0, q) = -\arctan[\omega\gamma/(q_0^2 - \omega^2)]$ the "spectral distribution" does not correspond to a Lorentzian (Breit-Wigner) function as naively expected, but to a "squared Lorentzian"

$$\frac{q_0(\omega\gamma)^3}{[(q_0^2 - \omega^2)^2 + (\omega\gamma)^2]^2} \quad (10)$$

See, e.g., Vanderheyden & Baym (1998); Morozov & Röpke, Ann. Phys. 324 (2009) 1261

Approximately selfconsistent HTL resumm. QCD

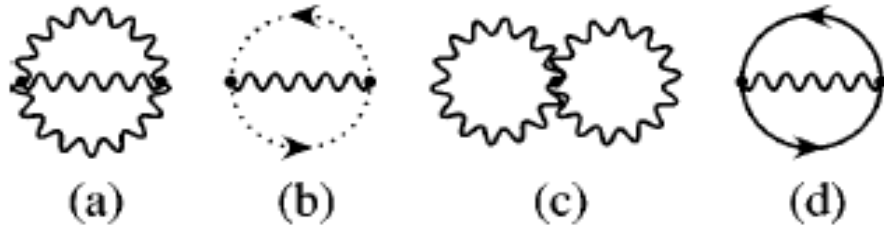


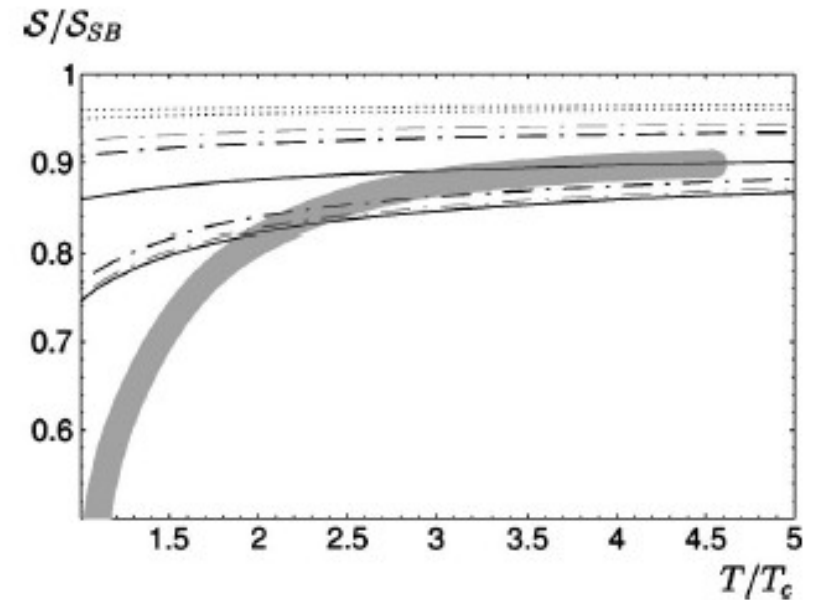
FIG. 3. Diagrams for Φ at 2-loop order in QCD. Wiggly, plain, and dotted lines refer respectively to gluons, quarks, and ghosts.

In ghost-free gauge, HTL resummed QCD thermodyn.

$$S_2 = -\frac{g^2 N_g T}{48} \left\{ \frac{4N + 5N_f}{3} T^2 + \frac{3N_f}{\pi^2} \mu^2 \right\},$$

$$N_2 = -\frac{g^2 \mu N_g N_f}{16\pi^2} \left(T^2 + \frac{\mu^2}{\pi^2} \right),$$

$$P_2 = -\frac{g^2 N_g}{32} \left\{ \frac{4N + 5N_f}{18} T^4 + \frac{N_f}{\pi^2} \mu^2 T^2 + \frac{N_f}{2\pi^4} \mu^4 \right\}$$



Generalized Optical Theorems

See derivations for T-matrices by R. Zimmermann & H. Stolz, pss (b) 131, 151 (1985)
 Here we consider the analogue of $T^{-1} = V^{-1} - G_2^0$, the propagator $S^{-1} = G^{-1} - \Pi$, G real, static

Assuming the inverse exists we have two identities: $S = S^* S^{*-1} S$ and $S^* = S^* S^{-1} S$

$$\begin{aligned} S_R + iS_I &= S^*(S_R^{-1} - iS_I^{-1})S, & \longrightarrow & & S_R &= S^*S_R^{-1}S, \\ S_R - iS_I &= S^*(S_R^{-1} + iS_I^{-1})S. & & & S_I &= -S^*S_I^{-1}S, \end{aligned}$$

With definition $S^{-1} = G^{-1} - \Pi$ follows off-shell optical theorem:

$$S_I = S^* \Pi_I S = S \Pi_I S^*$$

Using the fact that G is a real constant, we have: $(S_R^{-1})' = -\Pi'_R$ and $S_I^{-1} = -\Pi_I$

$$\begin{aligned} S'_R &= S^{*'} S_R^{-1} S + S^* (S_R^{-1})' S + S^* S_R^{-1} S' \\ &= S^{*'} \underbrace{(S_R^{-1} + iS_I^{-1} - iS_I^{-1})}_{S^{-1}} S + S^* (S_R^{-1})' S + S^* \underbrace{(S_R^{-1} - iS_I^{-1} + iS_I^{-1})}_{S^{*-1}} S' \\ &= \underbrace{S^{*'} + S'}_{2S'_R} - iS^{*'} S_I^{-1} S + iS^* S_I^{-1} S' + S^* (S_R^{-1})' S \\ &= S^* \Pi'_R S - iS^{*'} \Pi_I S + iS^* \Pi_I S', \end{aligned}$$

Derivative optical theorem:

$$S'_R \Pi_I = \underbrace{S^* \Pi'_R S \Pi_I}_{\Pi'_R S_I} + \underbrace{iS^{*'} \Pi_I S' \Pi_I - iS^* \Pi_I S \Pi_I}_{2 \operatorname{Im}[\Pi_I S \Pi_I S^{*'}]}, \quad \longrightarrow \quad S'_R \Pi_I - \Pi'_R S_I = 2 \operatorname{Im}[\Pi_I S \Pi_I S^{*'}]$$



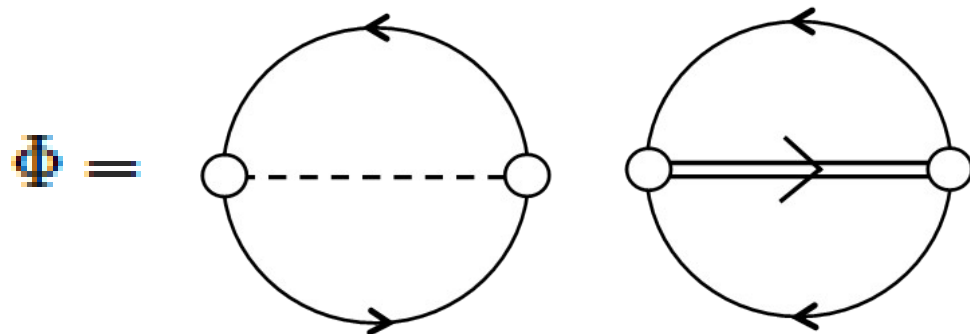
Φ-derivable Q-M-D PNJL model, 2-loop approximation

$$\Omega = \frac{1}{2} \frac{T}{V} \sum_{i=Q,M,D} c_i \text{Tr} \{ \ln [S_i^{-1}] + [S_i \Pi_i] \} + \Phi [S_Q, S_M, S_D] ,$$

$$S_i^{-1}(iz_n, \mathbf{q}) = S_{i,0}^{-1}(iz_n, \mathbf{q}) - \Pi_i(iz_n, \mathbf{q}) , \quad \frac{\delta \Omega}{\delta S_i} = 0 , \quad \text{if } \Pi_i = \frac{\delta \Omega}{\delta S_i} .$$

$$\Omega = \frac{1}{2} T \sum_{i=Q,M,D} \int \frac{d^3 q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} f_i(\omega) \text{Tr} \{ \text{Im} \ln [S_i^{-1}] + [\text{Re} S_i \text{Im} \Pi_i] \} + \tilde{\Omega}$$

$$\tilde{\Omega} = \Phi [S_Q, S_M, S_D] - \frac{1}{2} T \sum_{i=Q,M,D} \int \frac{d^3 q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} f_i(\omega) \text{Tr} \{ [\text{Im} S_i \text{Re} \Pi_i] \} ,$$



$$S = -\frac{\partial \Omega}{\partial T} = \sum_i S_i + \tilde{S}$$

$$N = -\frac{\partial \Omega}{\partial \mu} = \sum_i N_i + \tilde{N} .$$

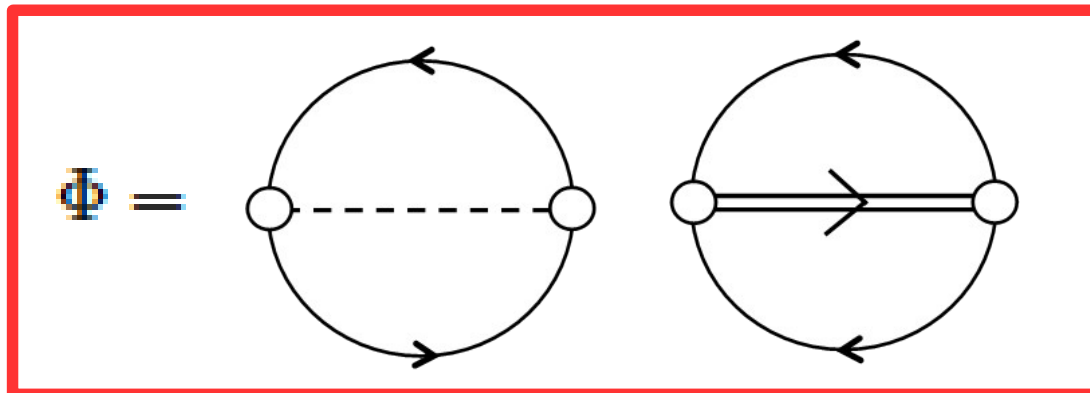
Φ -derivable Q-M-D PNJL model, 2-loop approximation

$$\Omega = \frac{1}{2V} \sum_{i=Q,M,D} c_i \text{Tr} \{ \ln [S_i^{-1}] + [S_i \Pi_i] \} + \Phi [S_Q, S_M, S_D] ,$$

$$S_i^{-1}(iz_n, \mathbf{q}) = S_{i,0}^{-1}(iz_n, \mathbf{q}) - \Pi_i(iz_n, \mathbf{q}) , \quad \frac{\delta \Omega}{\delta S_i} = 0 , \quad \text{if } \Pi_i = \frac{\delta \Omega}{\delta S_i} .$$

$$\Omega = \frac{1}{2} T \sum_{i=Q,M,D} \int \frac{d^3 q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} f_i(\omega) \text{Tr} \{ \text{Im} \ln [S_i^{-1}] + [\text{Re} S_i \text{Im} \Pi_i] \} + \tilde{\Omega}$$

$$\tilde{\Omega} = \Phi [S_Q, S_M, S_D] - \frac{1}{2} T \sum_{i=Q,M,D} \int \frac{d^3 q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} f_i(\omega) \text{Tr} \{ [\text{Im} S_i \text{Re} \Pi_i] \} ,$$



$$S = -\frac{\partial \Omega}{\partial T} = \sum_i S_i + \cancel{S}$$

$$N = -\frac{\partial \Omega}{\partial \mu} = \sum_i N_i + \cancel{N}$$

Φ -derivable Q-M-D PNJL model, 2-loop approximation

$$(\text{Im} \ln S^{-1})' = -\text{Im}(S\Pi') = \underbrace{S'_R \Pi_I - S_I \Pi'_R}_{2 \text{Im}(S\Pi_I S^{*'}\Pi_I)} - \underbrace{(\Pi_I S'_R + S_R \Pi'_I)}_{(\Pi_I S_R)'}$$

Use optical theorems ...

$$S\Pi_I = \sin \delta e^{i\delta}, \quad S^{*'}\Pi_I = -i\delta' \sin \delta e^{-i\delta}, \quad 2\text{Im}(S\Pi_I S^{*'}\Pi_I) = -2\delta' \sin^2 \delta.$$

Generalized Beth-Uhlenbeck EoS

$$\Omega = - \sum_{i=Q,M,D} d_i \int \frac{d^3q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} T \ln[1 - e^{-(\omega - \mu_i)/T}] \sin^2 \delta_i(\omega, \mathbf{q}) \frac{\partial \delta_i(\omega, \mathbf{q})}{\partial \omega}$$

Effect of the \sin^2 term ... example: Breit-Wigner ...

$$\delta_i(\omega) = -\arctan \left[\frac{\omega_i \Gamma_i}{\omega^2 - \omega_i^2} \right], \quad \frac{\partial \delta_i(\omega)}{\partial \omega} = \frac{2\omega \omega_i \Gamma_i}{(\omega^2 - \omega_i^2)^2 + \omega_i^2 \Gamma_i^2},$$

$$\sin^2 \delta_i(\omega) \frac{\partial \delta_i(\omega)}{\partial \omega} = \frac{2\omega (\omega_i \Gamma_i)^3}{[(\omega^2 - \omega_i^2)^2 + \omega_i^2 \Gamma_i^2]^2}.$$

“Squared Lorentzian” ...
 Vanderheyden & Baym (1998)
 Morozov & Roepke (2009)

1. Cluster expansion in the 2PI formalism

- Φ – derivable approach to the grand canonical thermodynamic potential
[Baym, Phys. Rev. 127 (1962) 139]

$$J = -\text{Tr} \{ \ln(-G_1) \} - \text{Tr} \{ \Sigma_1 G_1 \} + \text{Tr} \{ \ln(-G_2) \} + \text{Tr} \{ \Sigma_2 G_2 \} + \Phi[G_1, G_2]$$

with full propagators:

$G_1^{-1}(1, z) = z - E_1(p_1) - \Sigma_1(1, z)$; $G_2^{-1}(12, 1'2', z) = z - E_1(p_1) - E_2(p_2) - \Sigma_2(12, 1'2', z)$
and selfenergies

$$\Sigma_1(1, 1') = \frac{\delta\Phi}{\delta G_1(1, 1')} ; \Sigma_2(12, 1'2', z) = \frac{\delta\Phi}{\delta G_2^{-1}(12, 1'2', z)}.$$

Because of stationarity equivalent to

$$n = -\frac{1}{\Omega} \frac{\partial J}{\partial \mu} = \frac{1}{\Omega} \sum_1 \int_{-\infty}^{\infty} \frac{d\omega}{\pi} f_1(\omega) S_1(1, \omega),$$

(baryon number conservation)

- Generalization to A-nucleon clusters in nuclear matter

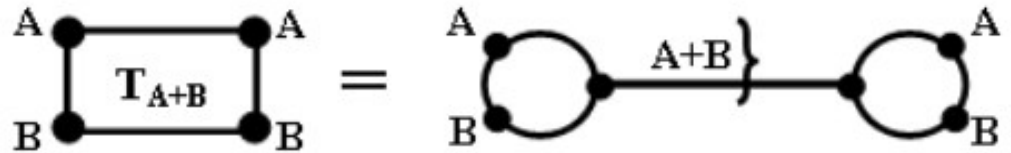
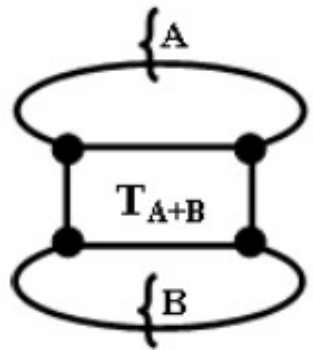
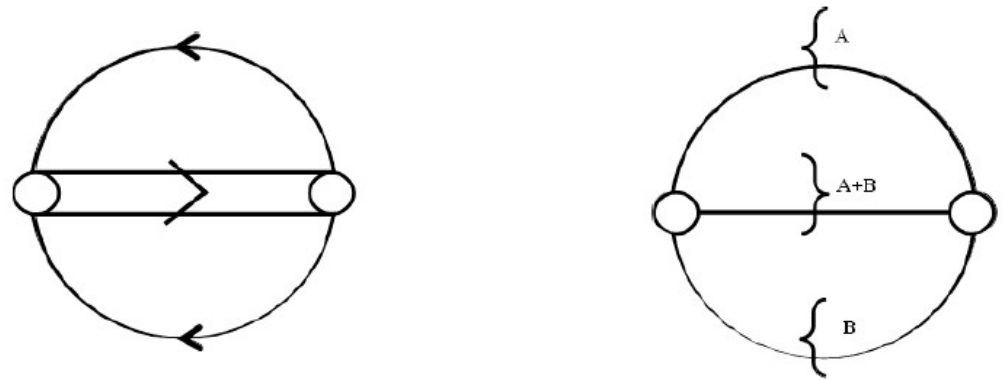
$$\Omega = \sum_A (-1)^A [\text{Tr} \ln (-G_A^{-1}) + \text{Tr} (\Sigma_A G_A)] + \Phi ,$$

$$G_A^{-1} = G_A^{(0)-1} - \Sigma_A , \quad \Sigma_A(1 \dots A, 1' \dots A', z_A) = \frac{\delta\Phi}{\delta G_A(1 \dots A, 1' \dots A', z_A)} .$$

1. Cluster expansion in the 2PI formalism

A) Choice of the Φ -functional:

- 2-particle irreducible diagrams
- closed 2-loop diagram involving 3 cluster propagators (A, B, A+B) and 2 vertices
- equivalent to 1 T-matrix + 2 propagators



B) Ansatz for thermodynamic potential:

$$\Omega = \sum_A (-1)^A [\text{Tr} \ln (-G_A^{-1}) + \text{Tr} (\Sigma_A G_A)] + \sum_{A,B} \Phi[G_A, G_B, G_{A+B}],$$

$$G_A^{-1} = G_A^{(0)-1} - \Sigma_A, \quad \Sigma_A(1 \dots A, 1' \dots A', z_A) = \frac{\delta \Phi}{\delta G_A(1 \dots A, 1' \dots A', z_A)}.$$

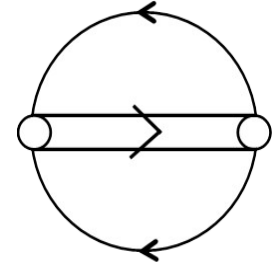
C) Check: conservation laws, e.g.:

(correspondence to GF formalism)

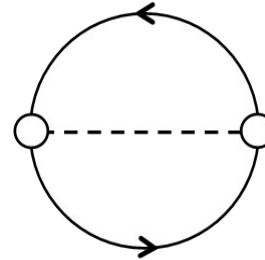
$$n = -\frac{1}{V} \frac{\partial \Omega}{\partial \mu} = \frac{1}{V} \sum_1 \int_{-\infty}^{\infty} \frac{d\omega}{\pi} f_1(\omega) A_1(1, \omega)$$

Cluster virial expansion in the 2PI formalism, Examples:

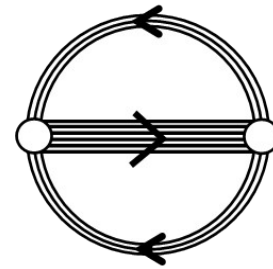
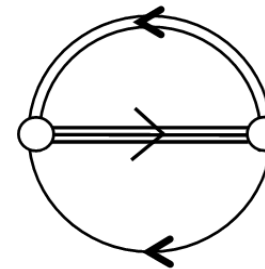
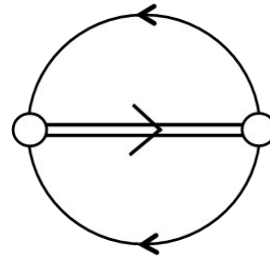
A) Deuterons in nuclear matter:



B) Mesons in quark matter:

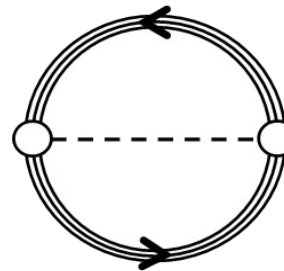
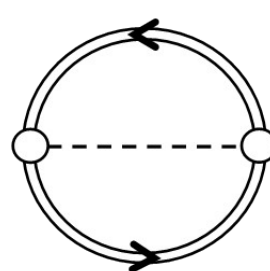


C) Nucleons in quark matter:



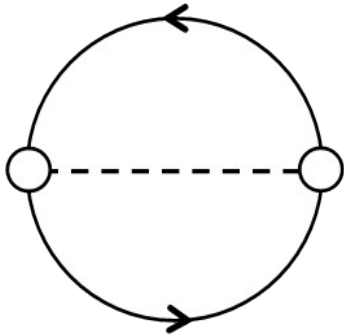
D) Nucleons and mesons (hadron resonance gas) in quark matter:

B) + C) +

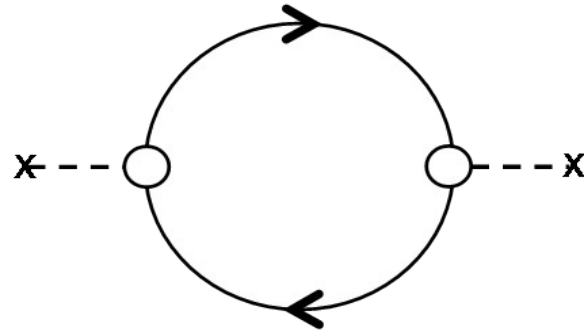


Example B: Mesons in quark matter

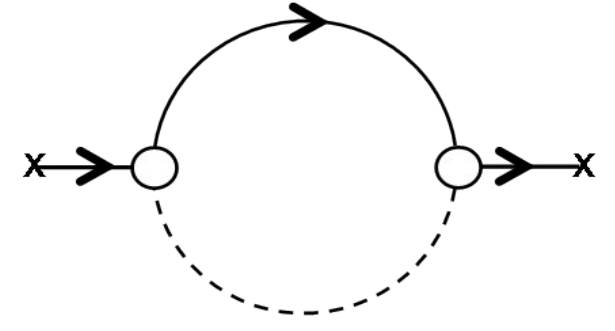
Φ -functional



Meson selfenergy (RPA)



Quark selfenergy



$$T_M^{-1}(q, \omega + i\eta) = G_S^{-1} - \Pi_M(q, \omega + i\eta) = |T_M(q, \omega)|^{-1} e^{-i\delta_M(q, \omega)}, \quad \delta_M(q, \omega) = \arctan(\Im T_M / \Re T_M)$$

$$\Omega = \Omega_{\text{MF}} + \Omega_M, \quad \sigma_{\text{MF}} = 2N_f N_c G_S \int \frac{d^3 p}{(2\pi)^3} \frac{m}{E_p} [1 - f_-(E_p) - f_+(E_p)],$$

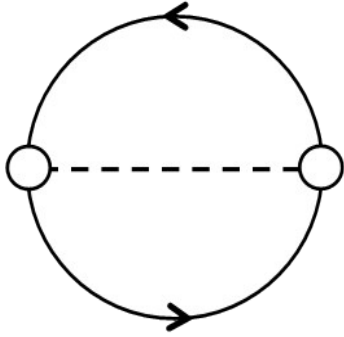
$$\Omega_{\text{MF}} = \frac{\sigma_{\text{MF}}^2}{4G_S} - 2N_c N_f \int \frac{d^3 p}{(2\pi)^3} \left[E_p + T \ln \left(1 + e^{-(E_p - \Sigma_+ - \mu)/T} \right) + T \ln \left(1 + e^{-(E_p + \Sigma_- + \mu)/T} \right) \right],$$

$$\Omega_M = d_M \int \frac{d^3 k}{(2\pi)^3} \int \frac{d\omega}{2\pi} \left\{ \omega + 2T \ln \left[1 - e^{-\omega/T} \right] 2 \sin^2 \delta_M(k, \omega) \frac{\delta_M(k, \omega)}{d\omega} \right\},$$

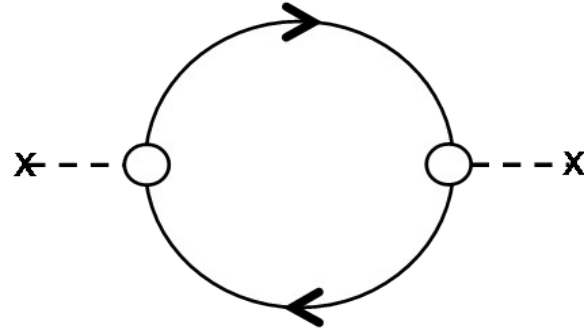
$$\Sigma_M(\mathbf{0}, p_0) = d_M \int \frac{d^4 q}{(2\pi)^4} \pi \rho_M(\mathbf{q}, q_0) \left\{ \frac{(\gamma_0 + m/E_q)[1 + g(q_0) - f_-(E_q)]}{q_0 - p_0 + E_q - \mu - i\eta} + \frac{(\gamma_0 - m/E_q)[g(q_0) + f_+(E_q)]}{q_0 - p_0 - E_q - \mu - i\eta} \right\},$$

Example B: Mesons in quark matter

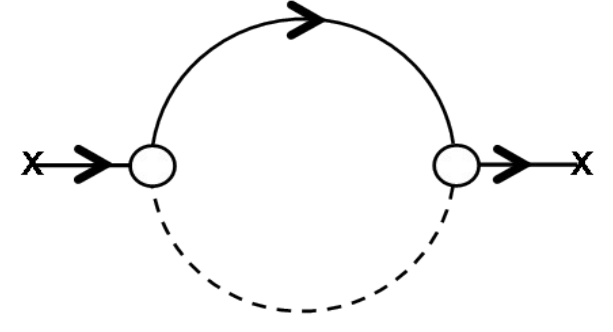
Φ -functional



Meson selfenergy (RPA)



Quark selfenergy



$$T_M^{-1}(q, \omega + i\eta) = G_S^{-1} - \Pi_M(q, \omega + i\eta) = |T_M(q, \omega)|^{-1} e^{-i\delta_M(q, \omega)}, \quad \delta_M(q, \omega) = \arctan(\Im T_M / \Re T_M)$$

$$\Omega = \Omega_{\text{MF}} + \Omega_M, \quad \sigma_{\text{MF}} = 2N_f N_c G_S \int \frac{d^3 p}{(2\pi)^3} \frac{m}{E_p} [1 - f_-(E_p) - f_+(E_p)],$$

$$\Omega_{\text{MF}} = \frac{\sigma_{\text{MF}}^2}{4G_S} - 2N_c N_f \int \frac{d^3 p}{(2\pi)^3} \left[E_p + T \ln \left(1 + e^{-(E_p - \Sigma_+ - \mu)/T} \right) + T \ln \left(1 + e^{-(E_p + \Sigma_- + \mu)/T} \right) \right],$$

$$\Omega_M = d_M \int \frac{d^3 k}{(2\pi)^3} \int \frac{d\omega}{2\pi} \left\{ \omega + 2T \ln \left[1 - e^{-\omega/T} \right] \boxed{2 \sin^2 \delta_M(k, \omega)} \frac{\delta_M(k, \omega)}{d\omega} \right\} \quad \boxed{\text{new !}}$$

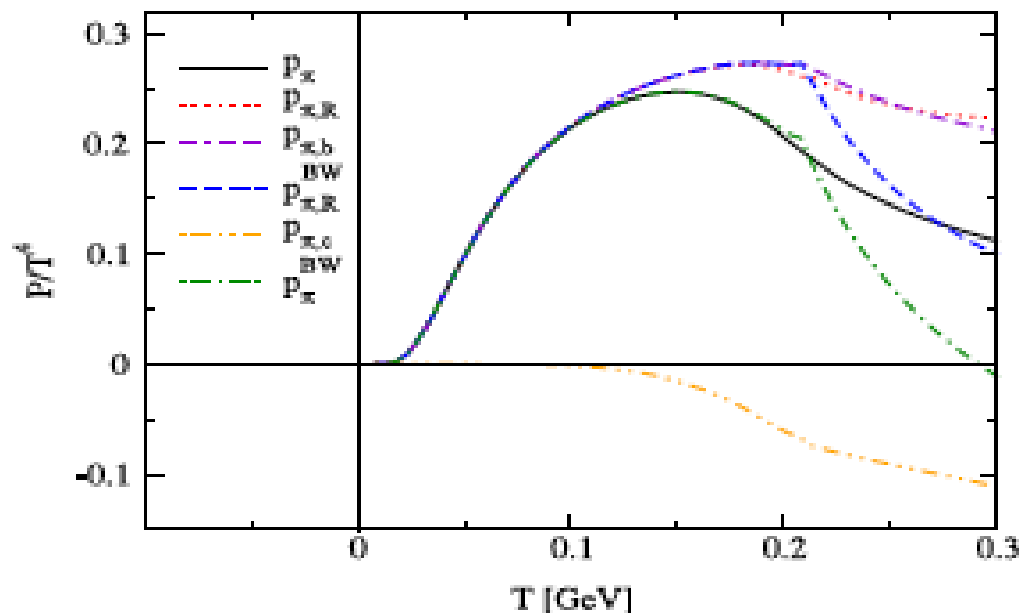
$$\Sigma_M(\mathbf{0}, p_0) = d_M \int \frac{d^4 q}{(2\pi)^4} \pi \rho_M(\mathbf{q}, q_0) \left\{ \frac{(\gamma_0 + m/E_q)[1 + g(q_0) - f_-(E_q)]}{q_0 - p_0 + E_q - \mu - i\eta} + \frac{(\gamma_0 - m/E_q)[g(q_0) + f_+(E_q)]}{q_0 - p_0 - E_q - \mu - i\eta} \right\}$$

Example B: Mesons in quark matter

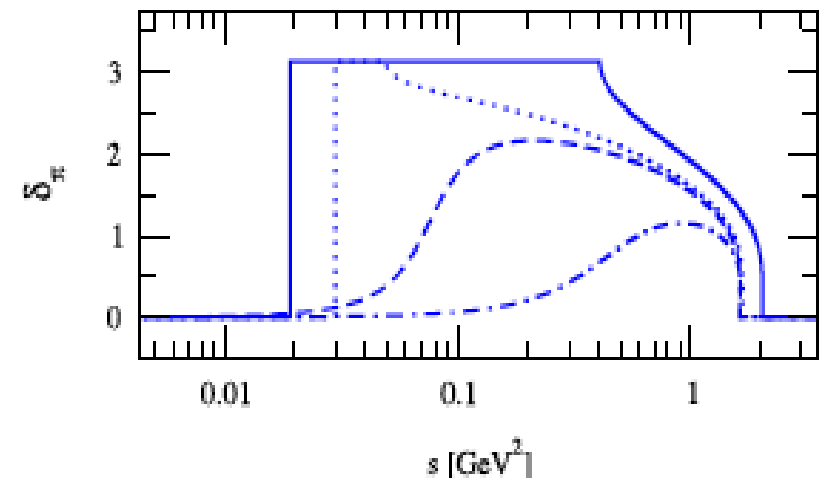
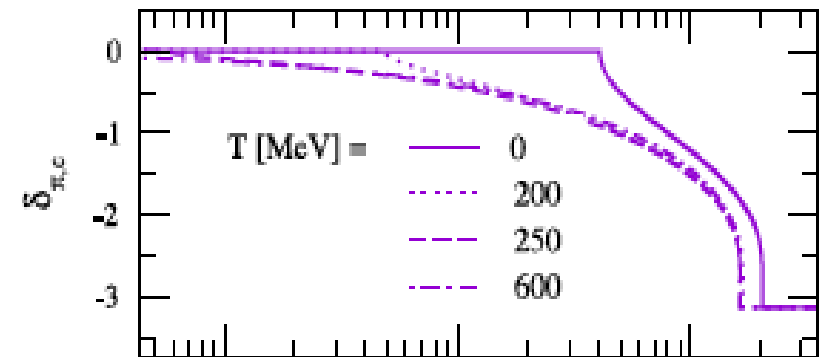
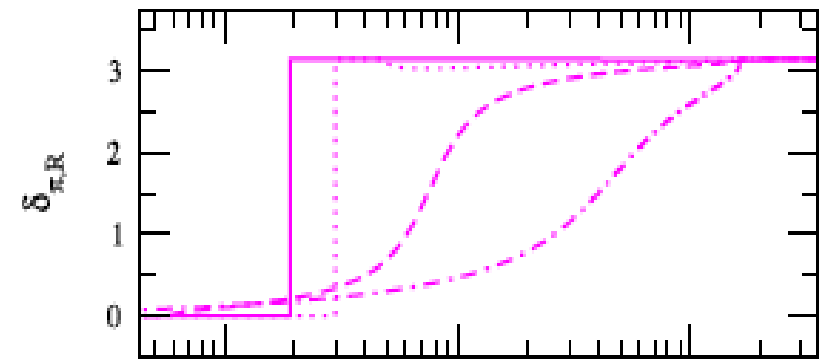
$$\Omega_X(T, \mu) = -d_X \int \frac{d^3q}{(2\pi)^3} \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} n_X^-(\omega) \delta_X(\omega, \mathbf{q}),$$

$$\int_0^{\infty} d\omega \frac{1}{\pi} \frac{d\delta_X(\omega; T)}{d\omega} = 0 = \underbrace{\int_0^{\omega_{\text{thr}}(T)} d\omega \frac{1}{\pi} \frac{d\delta_X(\omega; T)}{d\omega}}_{n_{B,X}(T)} + \underbrace{\frac{1}{\pi} \int_{\omega_{\text{thr}}(T)}^{\infty} d\omega \frac{d\delta_X(\omega; T)}{d\omega}}_{\frac{1}{\pi} [\delta_X(\infty; T) - \delta_X(\omega_{\text{thr}}; T)]},$$

$$p_\pi(T) = -d_\pi T \int \frac{d^3q}{(2\pi)^3} \int_0^{\infty} \frac{d\omega}{\pi} \ln(1 - e^{-\omega/T}) \frac{d\delta_\pi(\omega, \mathbf{q})}{d\omega}$$



$$\delta_\pi = \delta_{\pi,c} + \delta_{\pi,R}$$



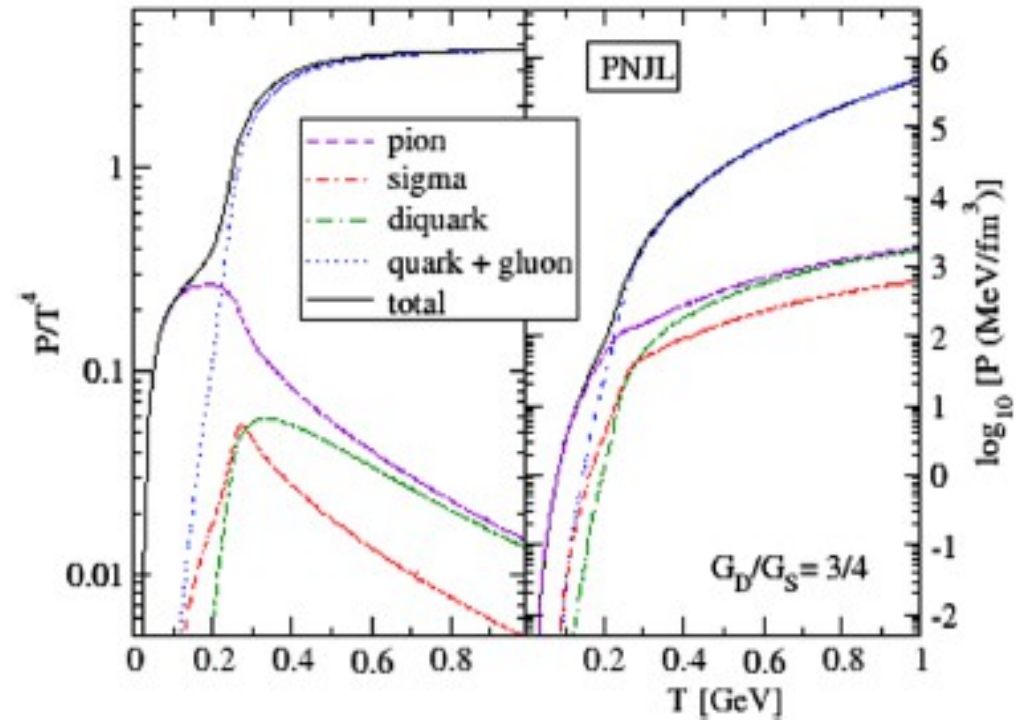
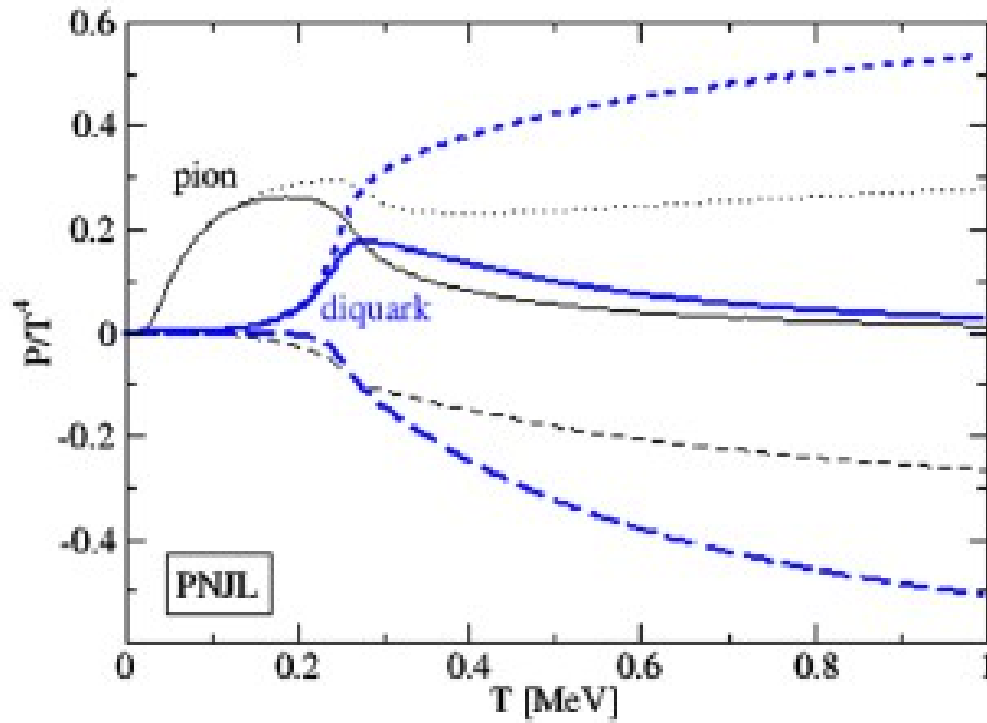
Example B*: Mesons+diquarks in quark matter

$$\Omega_Q = -\frac{2N_c N_f}{3} \int \frac{dp}{2\pi^2} \frac{p^4}{E_p} [f_{\bar{\Phi}}^+(E_p) + f_{\bar{\Phi}}^-(E_p)], \quad f_{\bar{\Phi}}^+(E_p) = \frac{(\bar{\Phi} + 2\Phi Y)Y + Y^3}{1 + 3(\bar{\Phi} + \Phi Y)Y + Y^3}, \quad Y = e^{-(E_p - \mu)/T}$$

$$\Omega_D = -3 \int \frac{d^3 p}{(2\pi)^3} \int \frac{d\omega}{2\pi} [g_{\bar{\Phi}}^+(\omega) + g_{\bar{\Phi}}^-(\omega)] \delta_D(\omega), \quad g_{\bar{\Phi}}^+(\omega) = \frac{(\Phi - 2\bar{\Phi} X)X + X^3}{1 - 3(\Phi - \bar{\Phi} X)X - X^3}, \quad X = e^{-(\omega - 2\mu)/T}$$

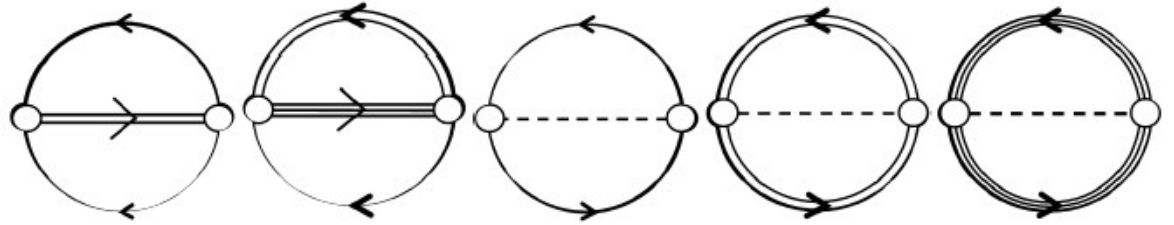
Suppression of colored states by Polyakov-loop Φ

Confinement: $\Phi=0$

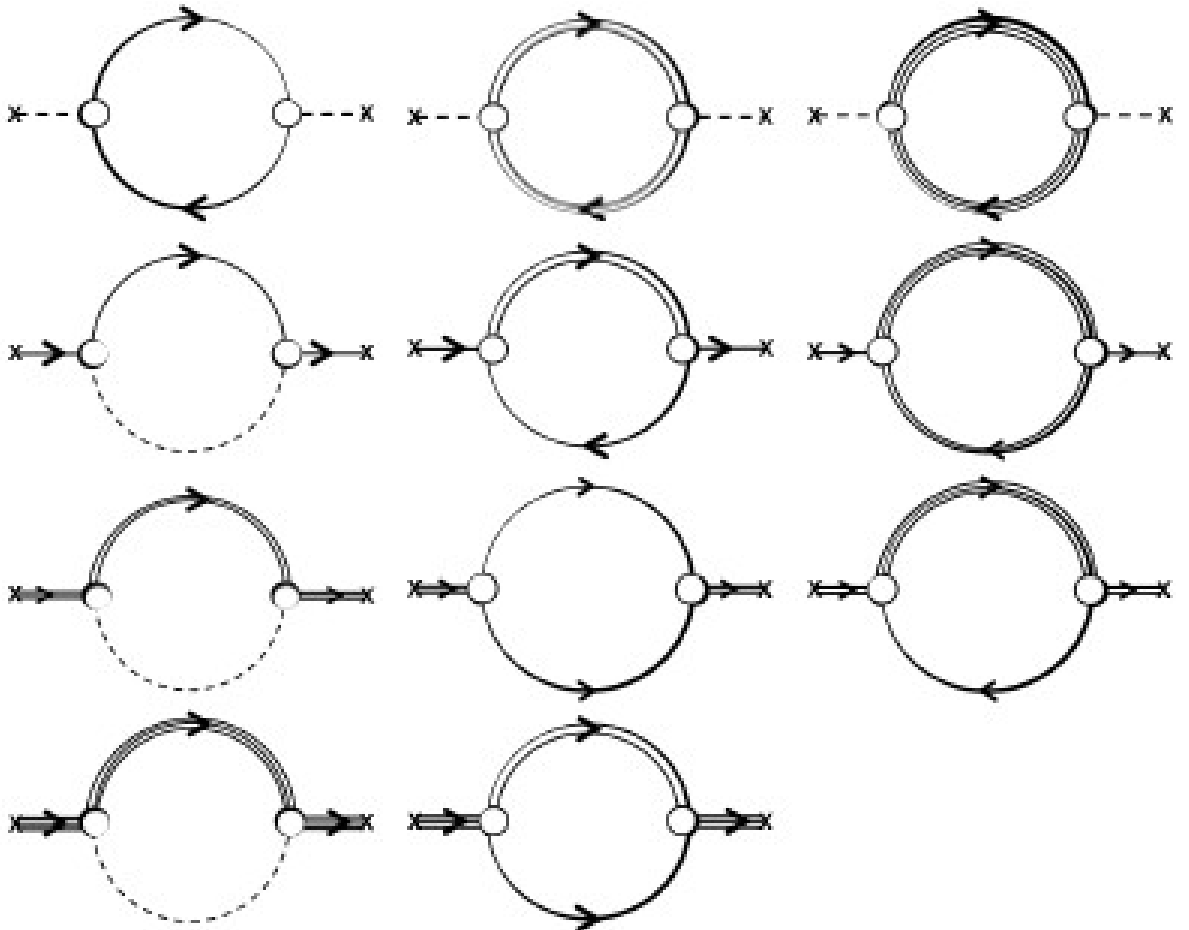


Example D: Hadron resonance gas – effect. model

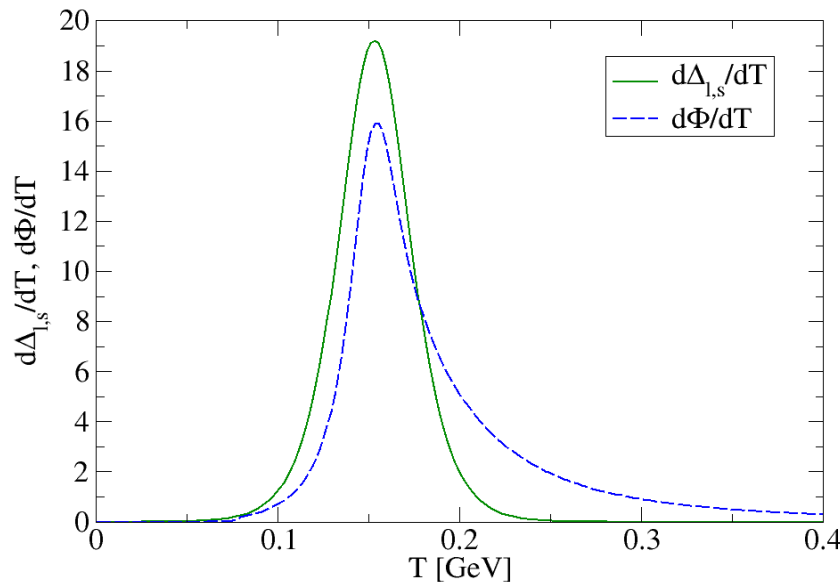
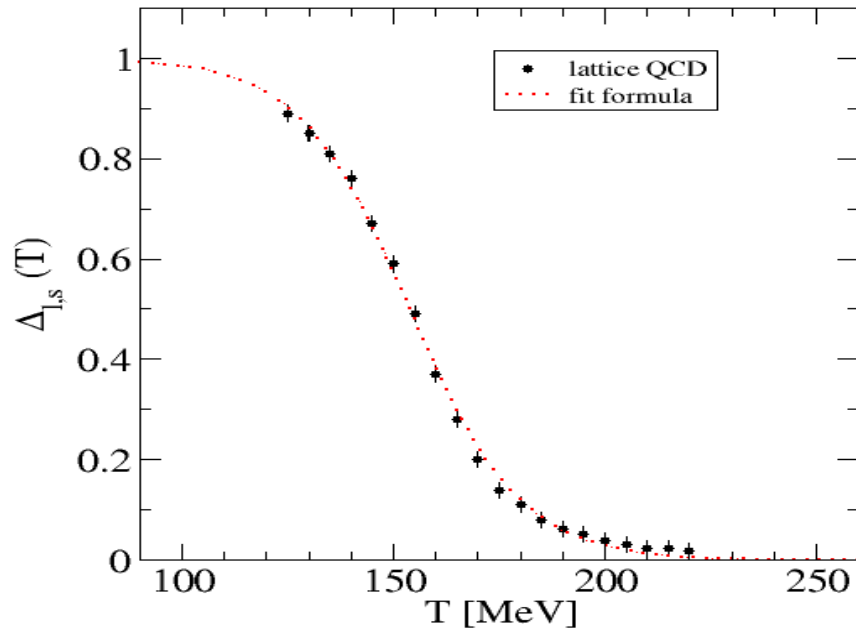
Φ -functional:



Selfenergies:



Example D: Mott HRG / PNJL – effective model



$$P_{\text{PNJL}}(T) = P_{\text{FG}}(T) + \mathcal{U}[\Phi; T] ,$$

$$P_{\text{FG}}(T) = 4 \sum_{\sigma=u,d,s} \int \frac{d^3p}{(2\pi)^3} T \ln [1 + 3\Phi(Y + Y^2) + Y^3]$$

$$Y(E_p) = \exp(-E_p/T)$$

$$\mathcal{U}[\Phi; T] = -\frac{a(T)}{2} \Phi^2 + b(T) \ln(1 - 6\Phi^2 + 8\Phi^3 - 3\Phi^4)$$

T-dependent quark masses from fit to LQCD

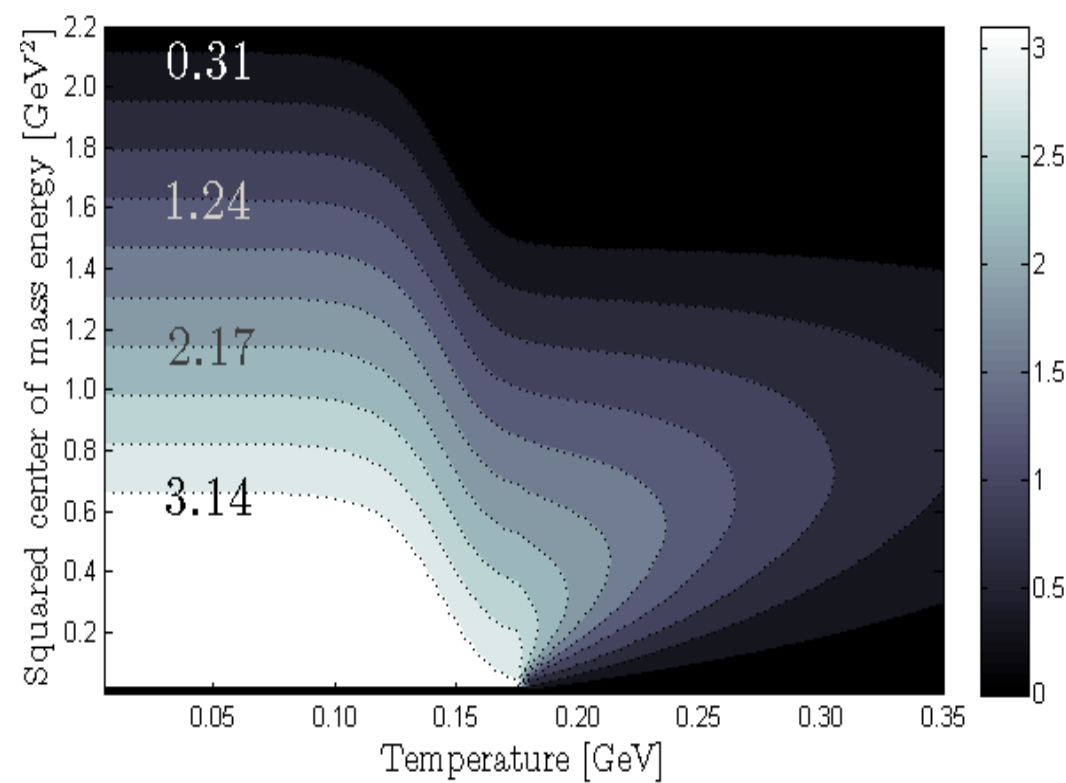
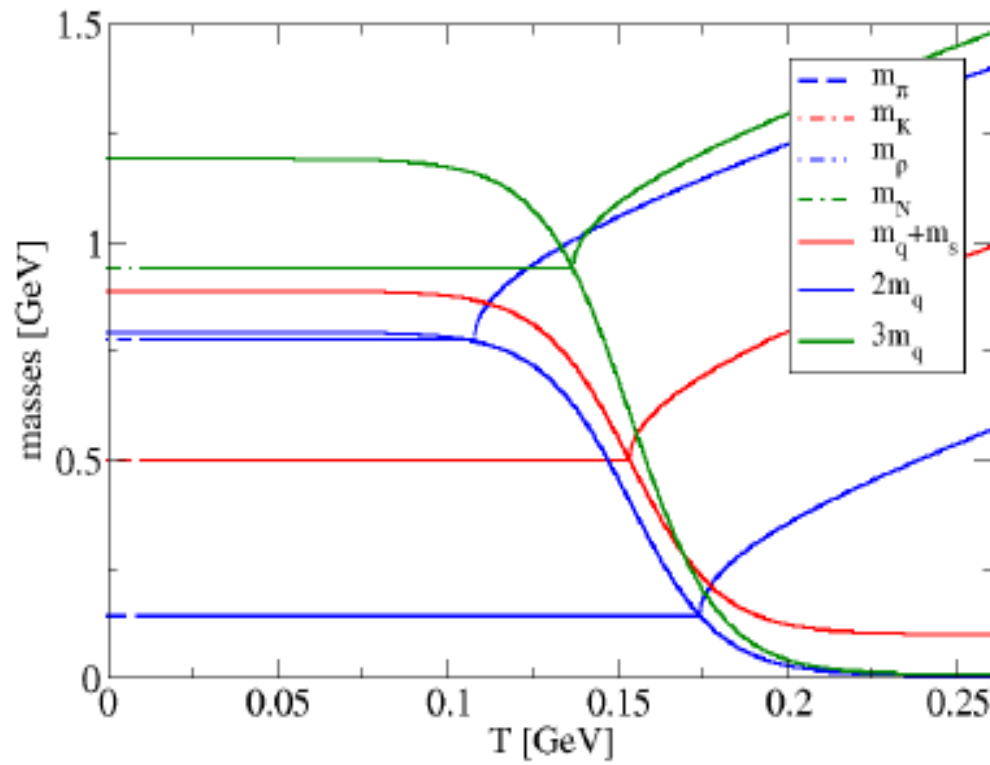
$$m(T) = [m(0) - m_0] \Delta_{l,s}(T) + m_0 ,$$

$$m_s(T) = m(T) + m_s - m_0 ,$$

$$\Delta_{l,s}(T) = \frac{1}{2} \left[1 - \tanh \left(\frac{T - T_c}{\delta_T} \right) \right]$$

$$T_c = 154 \text{ MeV} \quad \delta_T = 26 \text{ MeV}$$

Example D: Mott HRG / PNJL – effective model



Hadrons + Mott effect

$$P_i(T) = \mp d_i \int_0^\infty \frac{dp p^2}{2\pi^2} \int_0^\infty dM T \ln \left(1 \mp e^{-\sqrt{p^2 + M^2}/T} \right) \frac{2}{\pi} \sin^2 \delta_i(M^2; T) \frac{d\delta_i(M^2; T)}{dM}$$

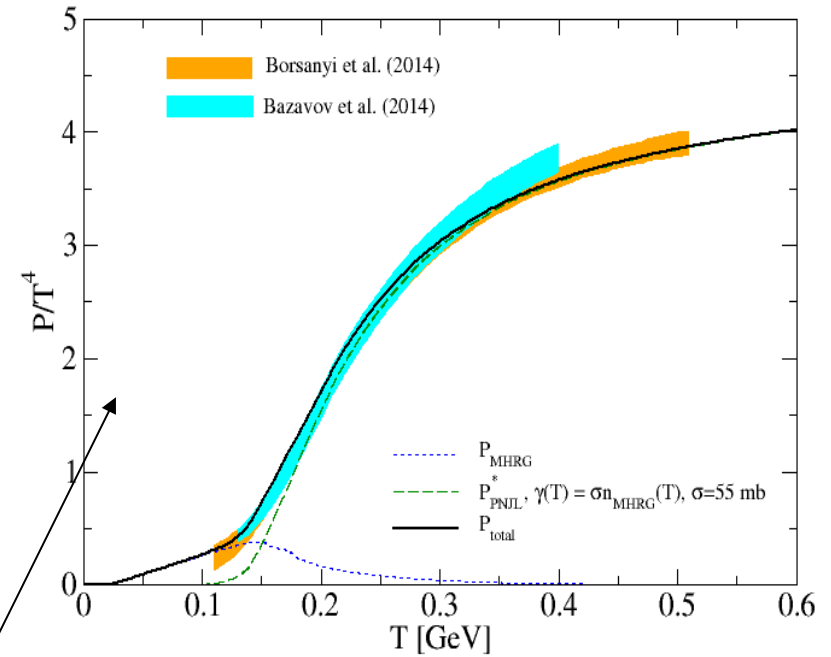
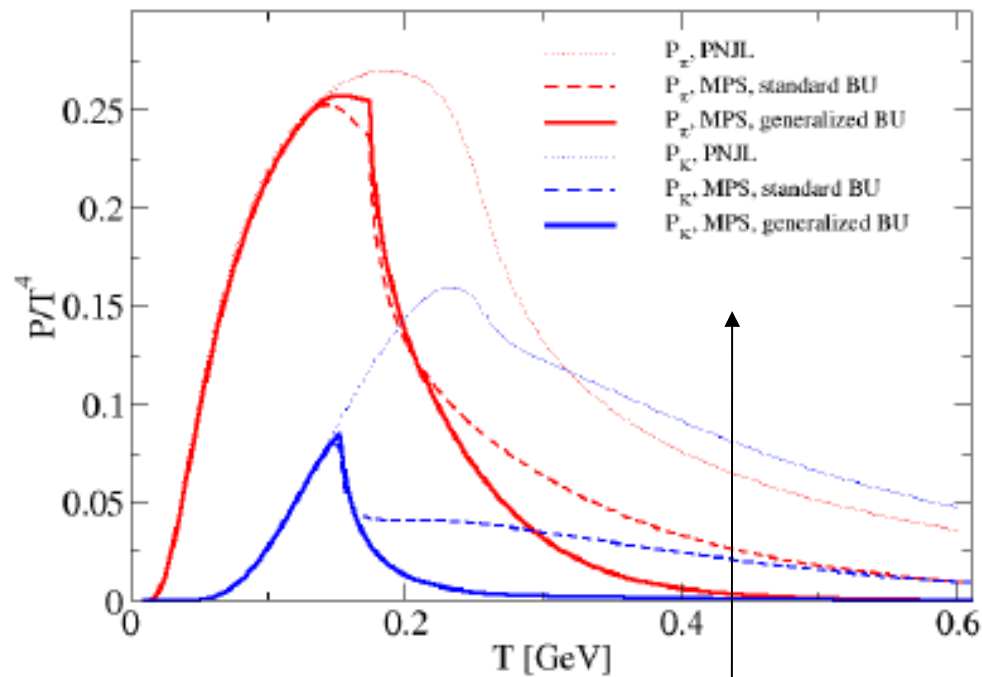
Quarks + rescattering effects

$$P_{FG}^*(T) = 4N_c \sum_{q=u,d,s} \int \frac{dp p^2}{2\pi^2} \int \frac{d\omega}{\pi} f_\Phi(\omega) \delta_q(\omega; \gamma),$$

$$f_\Phi(\omega) = \frac{\Phi(1 + 2Y)Y + Y^3}{1 + 3\Phi(1 + Y)Y + Y^3},$$

$$\delta_q(\omega; \gamma) = \frac{\pi}{2} + \arctan \left[\frac{\omega - \sqrt{p^2 + m_q^2}}{\gamma} \right]$$

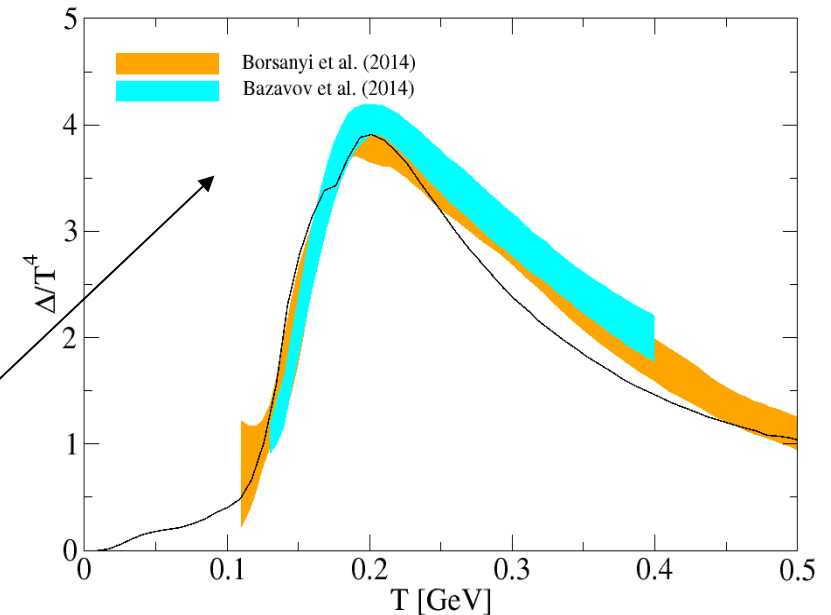
Example D: Mott HRG / PNJL – effective model



- Mott dissociation of hadrons (here pi, K) at the Chiral restoration temperature $T_c = 153$ MeV

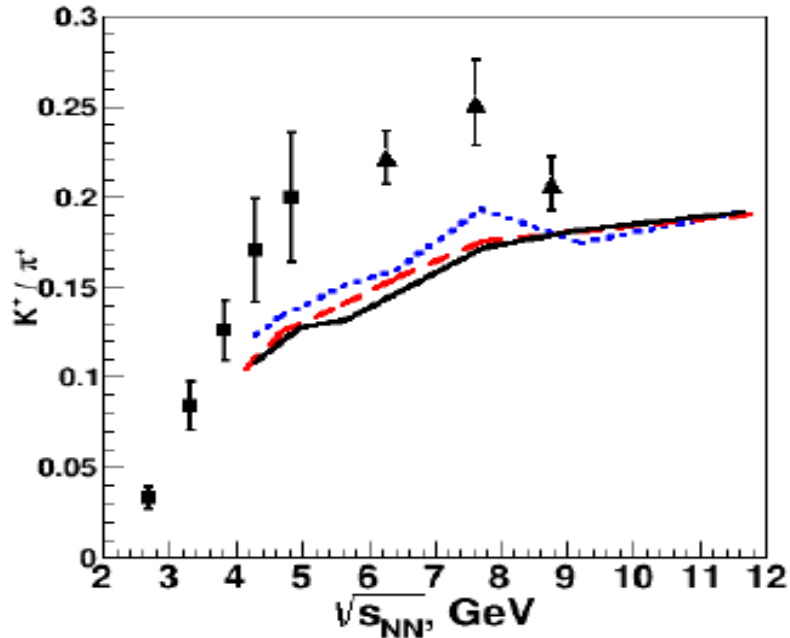
- Asymptotic behaviour of quark-gluon Pressure can be adjusted with rescattering Parameter gamma

- Very good correspondence between lattice QCD Thermodynamics and improved MHRG/PNJL model; Hadronic and partonic contributions quantified



What about K^+/π^+ (Marek's horn) in THESEUS ?

2-phase EoS, $b = 2$ fm



THESEUS simulation reproduces 3FH result, Thus it has the same discrepancy with experiment

--> some key element still missing in the program

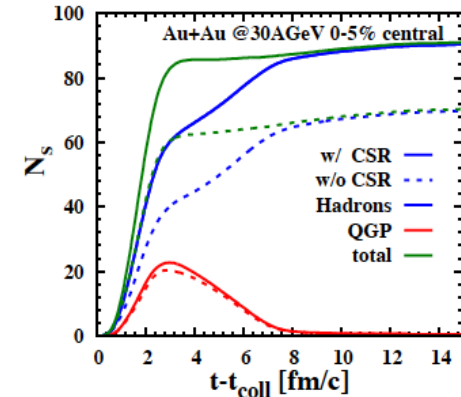
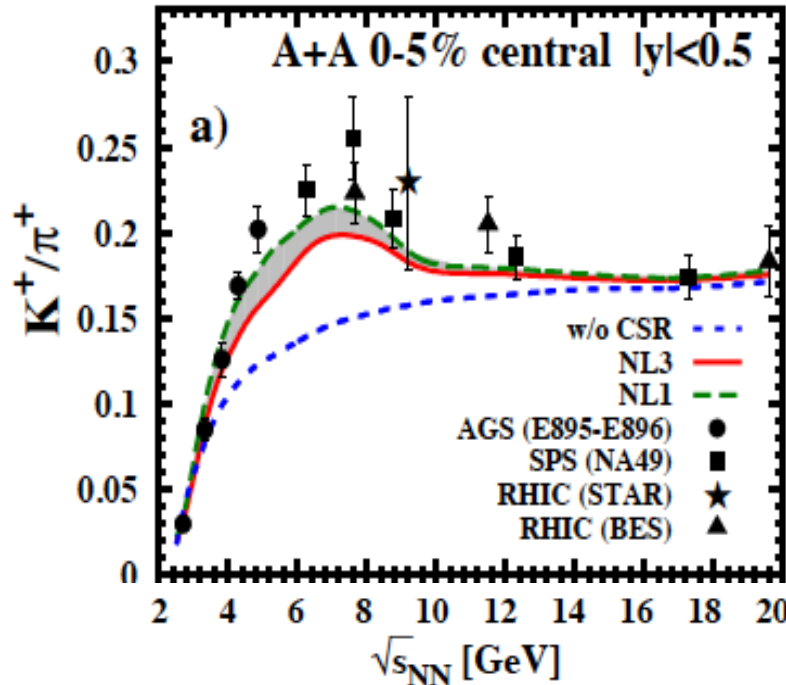
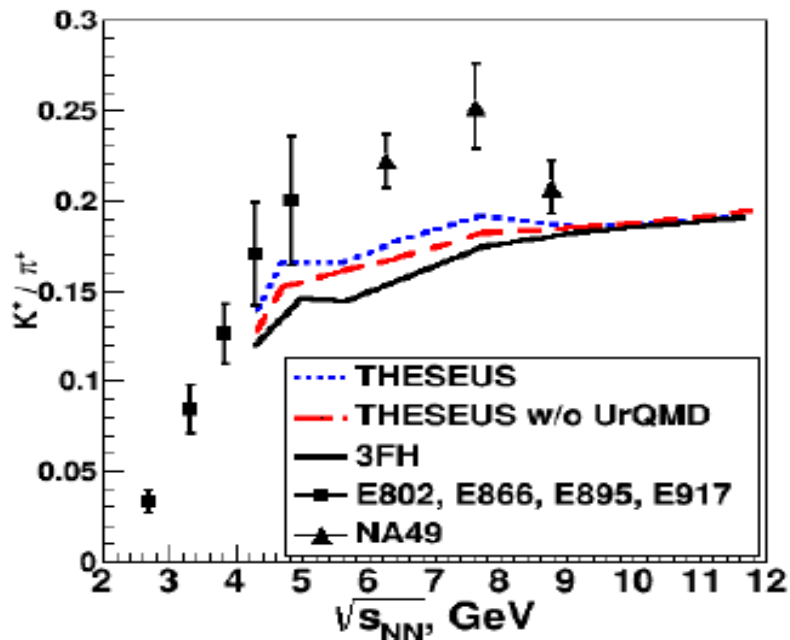
Batyuk, D.B., Bleicher, et al., PRC 94, 044917 (2016)

Recent new development in PHSD

Chiral symmetry restoration in HIC at intermediate ..."

A. Palmese et al., arxiv: 1607.04073; PRC 94, 044912

crossover EoS, $b = 2$ fm



Strange particle number increase by CSR

Mott dissociation of π and K in hot, dense quark matter

D. Blaschke, A. Dubinin, A. Radzhabov, A. Wergieluk, arxiv:1608.05383



Andrey Radzhabov in front of the University of Wrocław

PNJL model for $N_f=2+1$ quark matter with π and K

$$\mathcal{L} = \bar{q} (i\gamma^\mu D_\mu + \hat{m}_0) q + G_S \sum_{a=0}^8 \left[(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5\lambda^a q)^2 \right] - \mathcal{U}(\Phi[A], \bar{\Phi}[A]; T)$$

$$\Pi_{ff'}^{M^a}(q_0, \mathbf{q}) = 2N_c T \sum_n \int \frac{d^3p}{(2\pi)^3} \text{tr}_D \left[S_f(p_n, \mathbf{p}) \Gamma_{ff'}^{M^a} S_{f'}(p_n + q_0, \mathbf{p} + \mathbf{q}) \Gamma_{ff'}^{M^a} \right]$$

$$\Gamma_{ff'}^{P^a} = i\gamma_5 T_{ff'}^a, \quad \Gamma_{ff'}^{S^a} = T_{ff'}^a, \quad T_{ff'}^a = \begin{cases} (\lambda_3)_{ff'}, \\ (\lambda_1 \pm i\lambda_2)_{ff'} / \sqrt{2}, \\ (\lambda_4 \pm i\lambda_5)_{ff'} / \sqrt{2}, \\ (\lambda_6 \pm i\lambda_7)_{ff'} / \sqrt{2}, \end{cases}$$

$$P^a = \pi^0, \pi^\pm, K^\pm, K^0, \bar{K}^0$$

$$\Pi_{ff'}^{P^a, S^a}(q_0 + i\eta, \mathbf{0}) = 4 \left\{ I_1^f(T, \mu_f) + I_1^{f'}(T, \mu_{f'}) \mp [(q_0 + \mu_{ff'})^2 - (m_f \mp m_{f'})^2] I_2^{ff'}(z, T, \mu_{ff'}) \right\}$$

$$I_1^f(T, \mu_f) = \frac{N_c}{4\pi^2} \int_0^\Lambda \frac{dp p^2}{E_f} \left(n_f^- - n_f^+ \right),$$

$$I_2^{ff'}(z, T, \mu_{ff'}) = \frac{N_c}{4\pi^2} \int_0^\Lambda \frac{dp p^2}{E_f E_{f'}} \left[\frac{E_{f'}}{(z - E_f - \mu_{ff'})^2 - E_{f'}^2} n_f^- - \frac{E_{f'}}{(z + E_f - \mu_{ff'})^2 - E_{f'}^2} n_f^+ + \frac{E_f}{(z + E_{f'} - \mu_{ff'})^2 - E_f^2} n_{f'}^- - \frac{E_f}{(z - E_{f'} - \mu_{ff'})^2 - E_f^2} n_{f'}^+ \right]$$

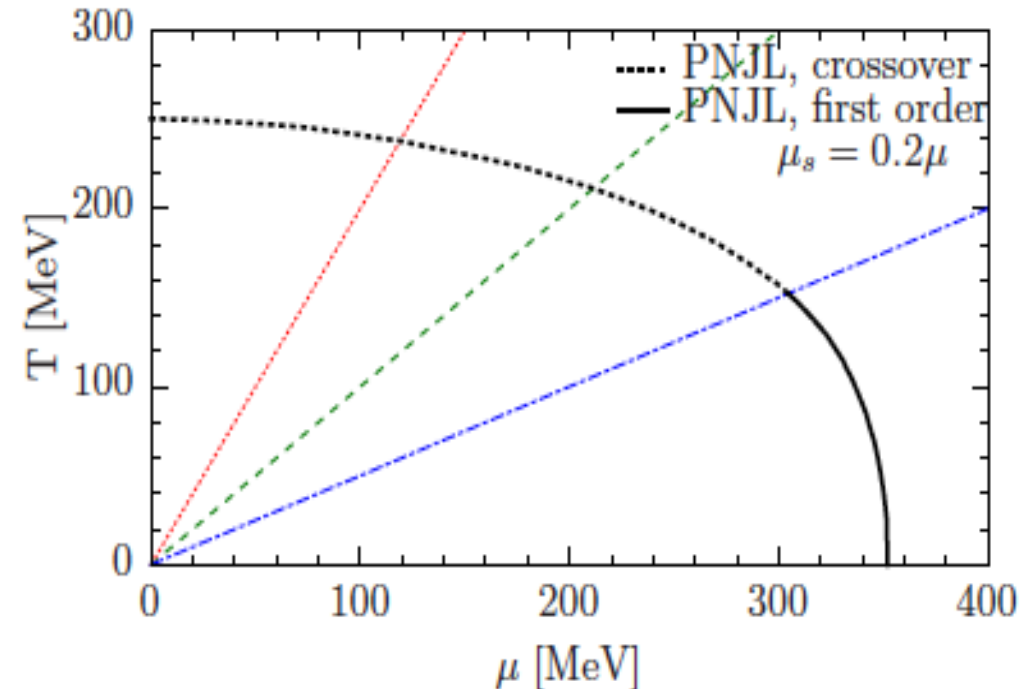
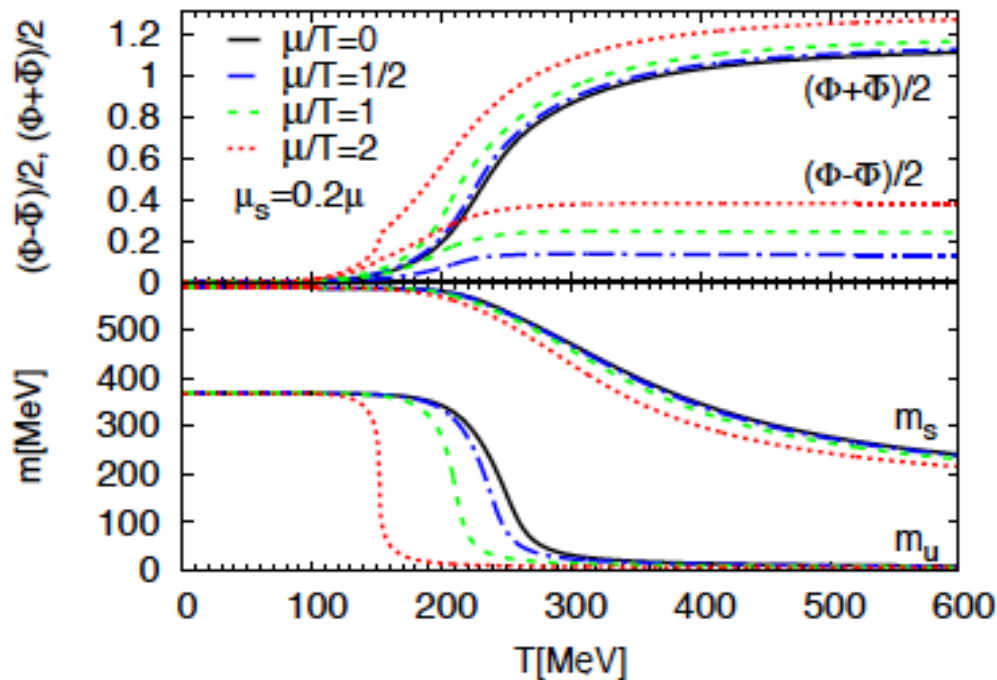
PNJL model for $N_f=2+1$ quark matter with π and K

$$m_f = m_{0,f} + 16 m_f G_S I_1^f(T, \mu), \quad \mathcal{P}_{ff'}^{M^a}(M_{M^a} + i\eta, \mathbf{0}) = 1 - 2G_S \Pi_{ff'}^{M^a}(M_{M^a} + i\eta, \mathbf{0}) = 0.$$

$$P_f = -\frac{(m_f - m_{0,f})^2}{8G} + \frac{N_c}{\pi^2} \int_0^\Lambda dp p^2 E_f + \frac{N_c}{3\pi^2} \int_0^\infty \frac{dp p^4}{E_f} [f_\Phi^+(E_f) + f_\Phi^-(E_f)]$$

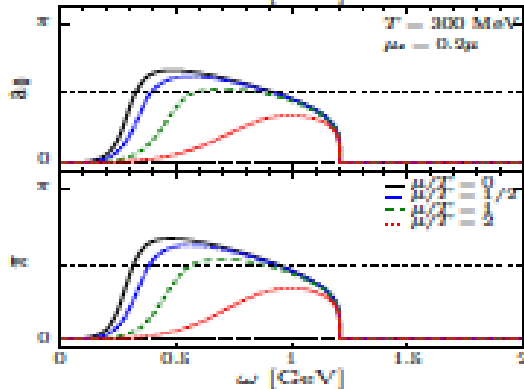
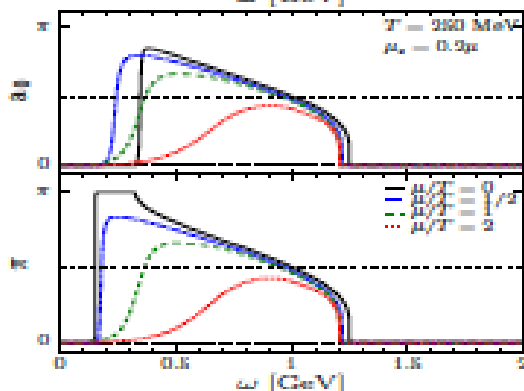
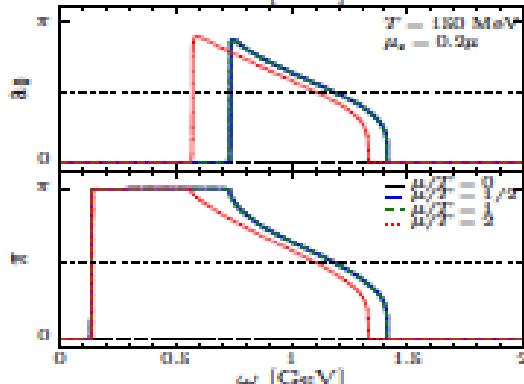
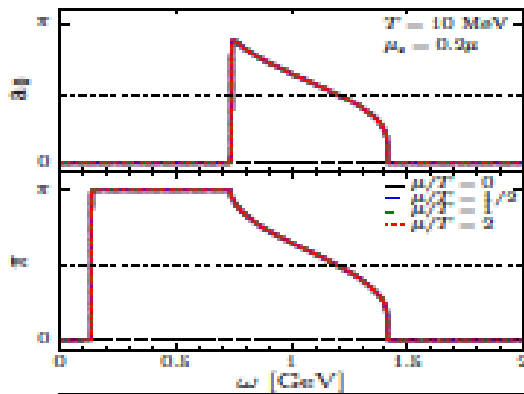
$$P_M = d_M \int \frac{d^3q}{(2\pi)^3} \int_0^\infty \frac{d\omega}{2\pi} \left\{ g(\omega - \mu_M) + g(\omega + \mu_M) \right\} \delta_M(\omega, \mathbf{q})$$

$$\delta_M(\omega, \mathbf{q}) = -\arctan \left\{ \frac{\text{Im} \left(\mathcal{P}_{ff'}^M(\omega - i\eta, \mathbf{q}) \right)}{\text{Re} \left(\mathcal{P}_{ff'}^M(\omega + i\eta, \mathbf{q}) \right)} \right\}$$



Mott dissociation of pions and kaons in the Beth-Uhlenbeck approach ...

D.B., A. Dubinin, A. Radzhabov, A. Wergieluk, arxiv:1608.05383
 D.B., M. Buballa, A. Dubinin, G. Ropke, D. Zablocki, Ann. Phys. (2014)



Thermodynamics of resonances (M) via phase shifts

$$P_M = d_M \int \frac{d^3 q}{(2\pi)^3} \int_0^\infty \frac{ds}{4\pi} \frac{1}{\sqrt{s+q^2}} \left\{ g(\sqrt{s+q^2} - \mu_M) \right\} \delta_M(\sqrt{s}; T, \mu)$$

Polyakov-loop Nambu – Jona-Lasinio modell

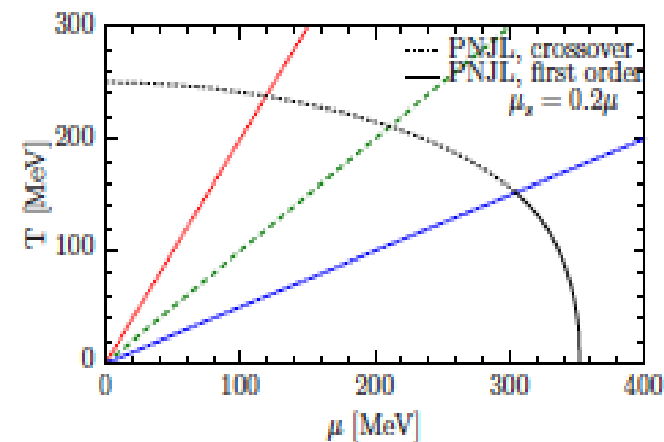
$$\Pi_{ff}^{M^*}(q_0, \mathbf{q}) = 2N_c T \sum_n \int \frac{d^3 p}{(2\pi)^3} \text{tr}_D \left[S_f(p_n, \mathbf{p}) \Gamma_{ff}^{M^*} S_{f'}(p_n + q_0, \mathbf{p} + \mathbf{q}) \Gamma_{ff'}^{M^*} \right],$$

$$\mathcal{P}_{ff'}^{M^*}(M_{M^*} + i\eta, \mathbf{0}) = 1 - 2G_S \Pi_{ff'}^{M^*}(M_{M^*} + i\eta, \mathbf{0})$$

$$\delta_M(\omega, \mathbf{q}) = -\arctan \left\{ \frac{\text{Im} \left(\mathcal{P}_{ff'}^M(\omega - i\eta, \mathbf{q}) \right)}{\text{Re} \left(\mathcal{P}_{ff'}^M(\omega + i\eta, \mathbf{q}) \right)} \right\}$$

Evaluation along trajectories $\mu/T = \text{const}$ in the phase diagram:

- Pion and a0 as partner states,
- Chiral symmetry restoration,
- Mott dissociation of bound states,
- Levinson theorem



Mott dissociation of pions and kaons in the Beth-Uhlenbeck approach ...

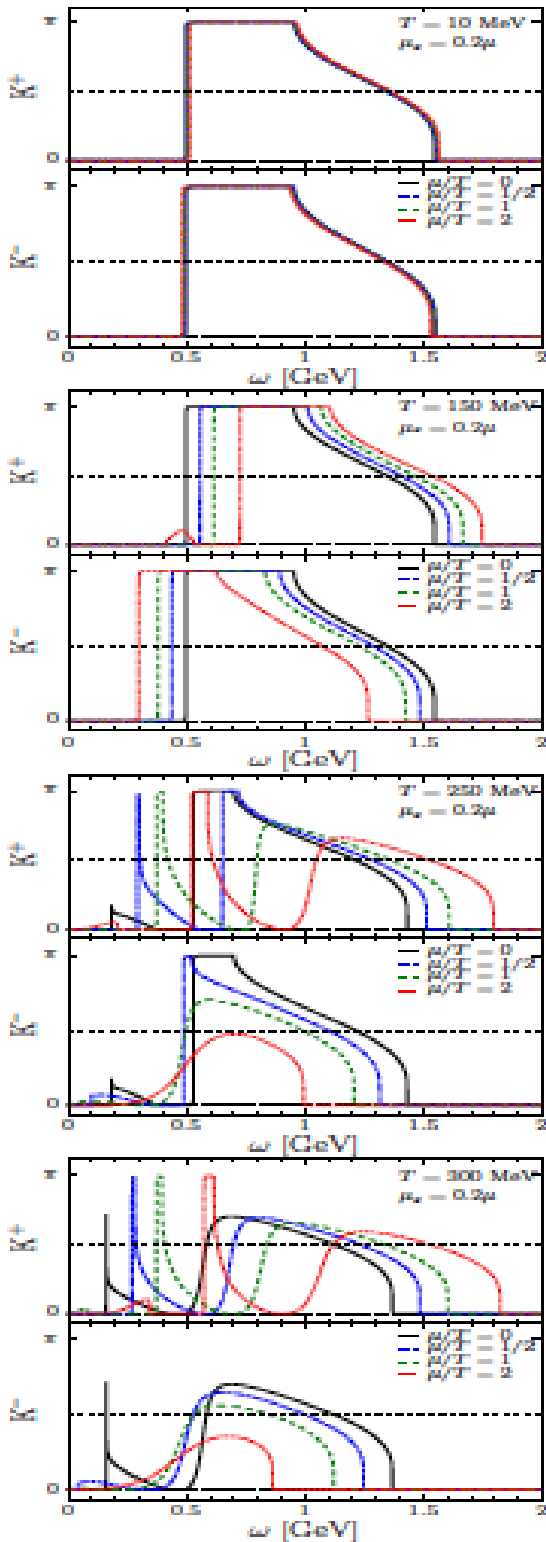
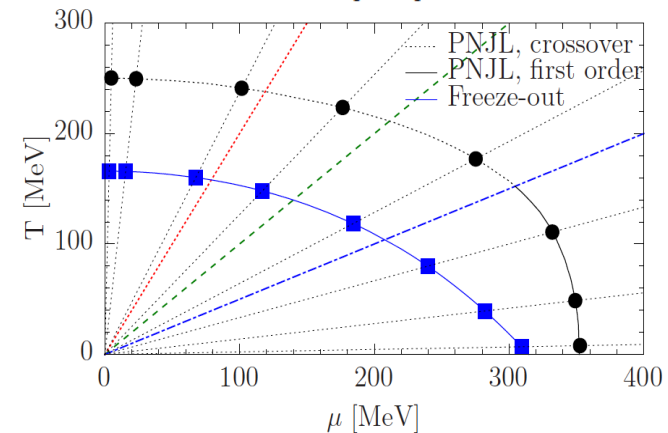
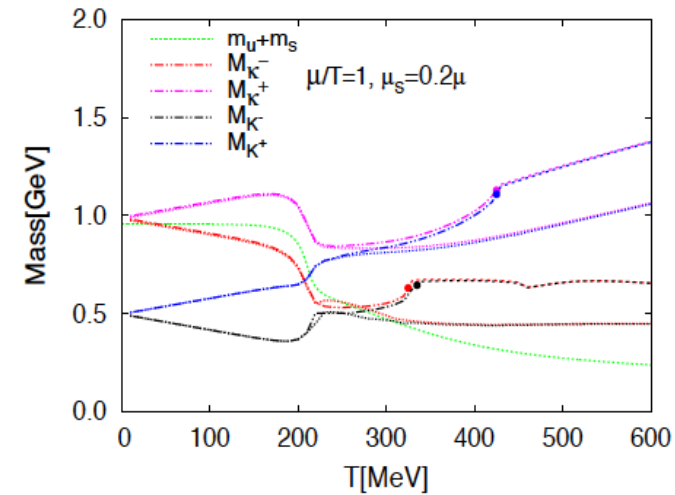
D.B., A. Dubinin, A. Radzhabov, A. Wergieluk, arxiv:1608.05383

Polarization loop in Polyakov-loop Nambu – Jona-Lasinio model

$$\Pi_{ff'}^{P^a, S^a}(q_0 + i\eta, \mathbf{0}) = 4\{I_1^f(T, \mu_f) + I_1^{f'}(T, \mu_{f'})\} \mp [(q_0 + \mu_{ff'})^2 - (m_f \mp m_{f'})^2] I_2^{ff'}(z, T, \mu_{ff'})$$

$$I_1^f(T, \mu_f) = \frac{N_c}{4\pi^2} \int_0^\Lambda \frac{dp p^2}{E_f} (n_f^- - n_f^+),$$

$$I_2^{ff'}(z, T, \mu_{ff'}) = \frac{N_c}{4\pi^2} \int_0^\Lambda \frac{dp p^2}{E_f E_{f'}} \left[\frac{E_{f'}}{(z - E_f - \mu_{ff'})^2 - E_{f'}^2} n_f^- - \frac{E_{f'}}{(z + E_f - \mu_{ff'})^2 - E_{f'}^2} n_f^+ + \frac{E_f}{(z + E_{f'} - \mu_{ff'})^2 - E_f^2} n_{f'}^- - \frac{E_f}{(z - E_{f'} - \mu_{ff'})^2 - E_f^2} n_{f'}^+ \right]$$

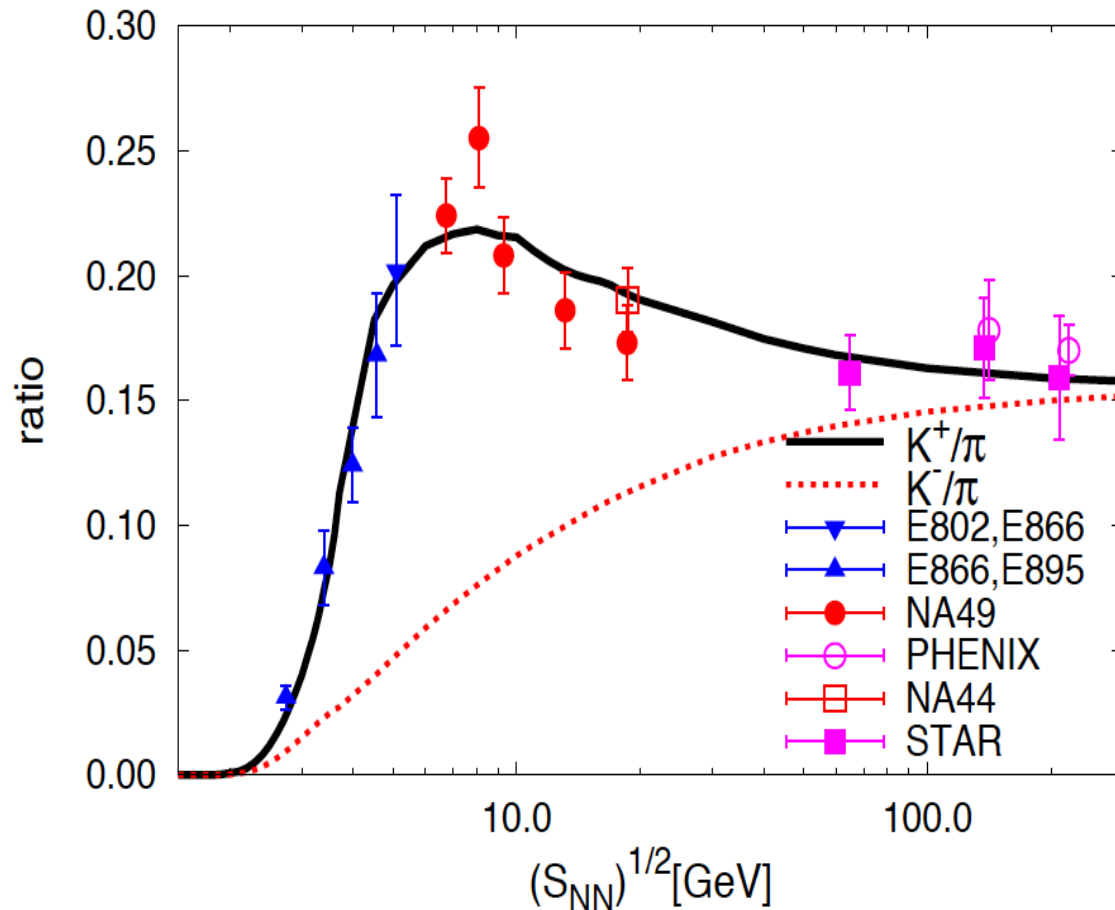


Anomalous low-mass mode for K+ in the dense medium !!

Mott dissociation of pions and kaons in Beth-Uhlenbeck: Explanation of the “horn” effect for K^+/π^+ in HIC?

Ratio of yields in BU approach
defined via phase shifts:

$$\frac{n_{K^\pm}}{n_{\pi^\pm}} = \frac{\int dM \int d^3p (M/E) g_{K^\pm}(E) [1 + g_{K^\pm}(E)] \delta_{K^\pm}(M)}{\int dM \int d^3p (M/E) g_{\pi^\pm}(E) [1 + g_{\pi^\pm}(E)] \delta_{\pi^\pm}(M)}$$



Evaluation along the freeze-out
Curve parametrized by Cleymans et al.

- enhancement for K^+ due to anomalous in-medium bound state mode
- no such enhancement for K^- or pions
- explore the effect in thermal statistical models and in THESEUS ...

D.B., A. Dubinin, A. Radzhabov,
A. Wergieluk, arxiv:1608.05383

Summary:

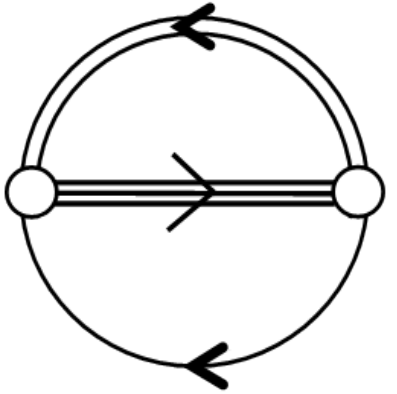
- GBU accounts consistently for hadron formation and dissociation (Mott effect)
In chiral Quark/Gluon models
- Comparison/calibration with lattice QCD data OK (shall be extended to finite μ)
- Fraction of hadronic correlations (bound and continuum) – input for models
- New modes in medium due to BSE dynamics (e.g., K^+)



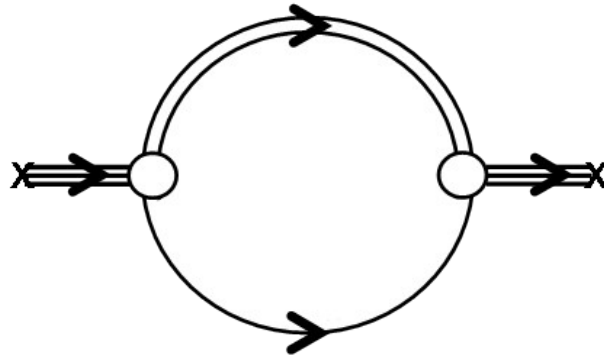
Additional Slides

Example C: Nucleons in quark matter

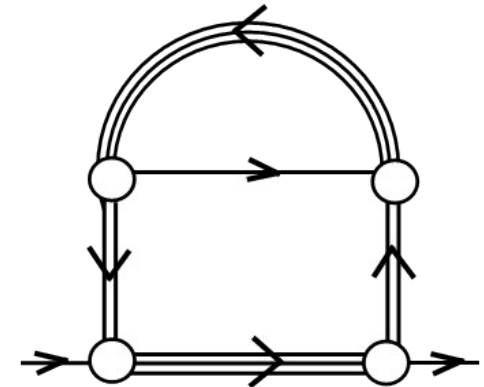
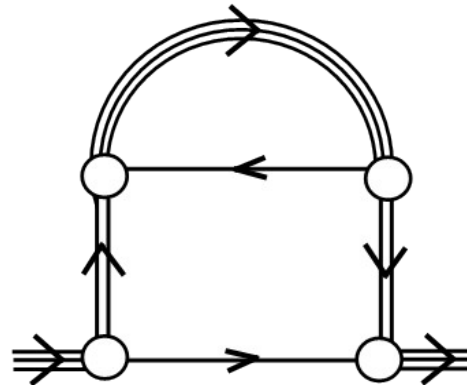
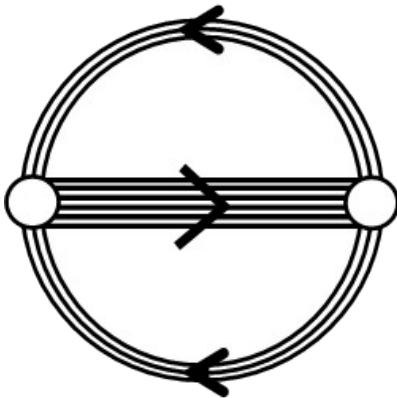
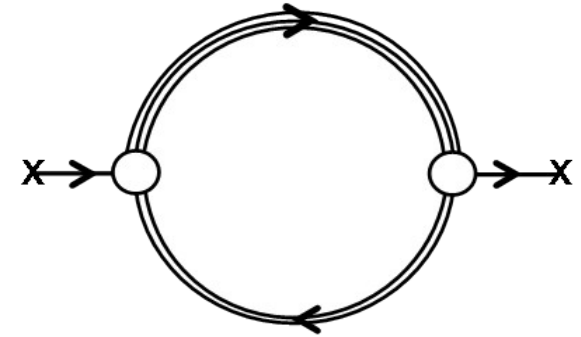
Φ -functional



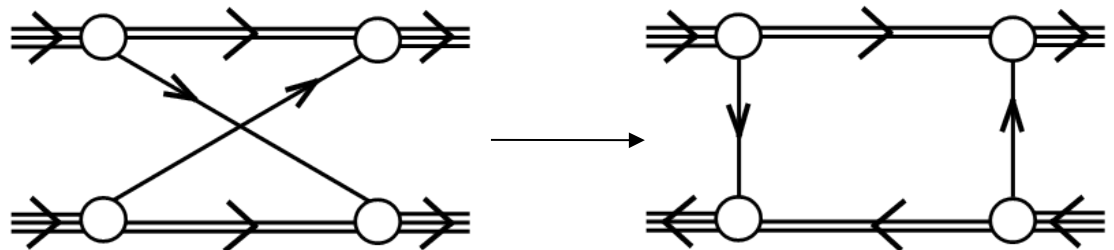
nucleon selfenergy



quark selfenergy

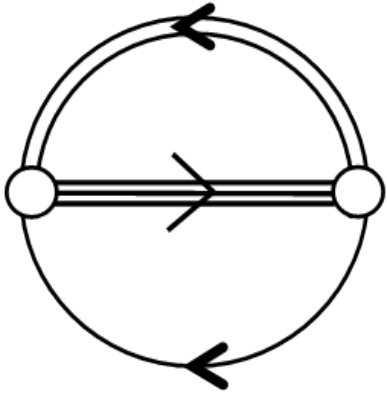


quark exchange interaction
between nucleons:

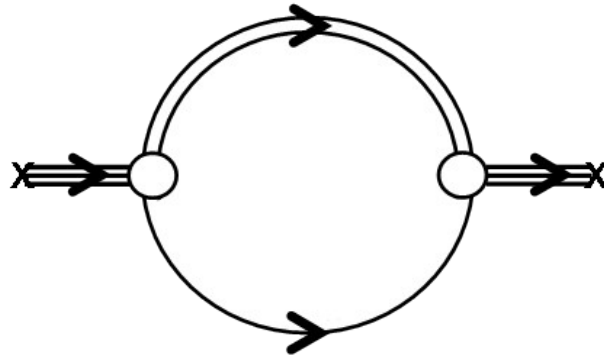


Example C: Nucleons in quark matter

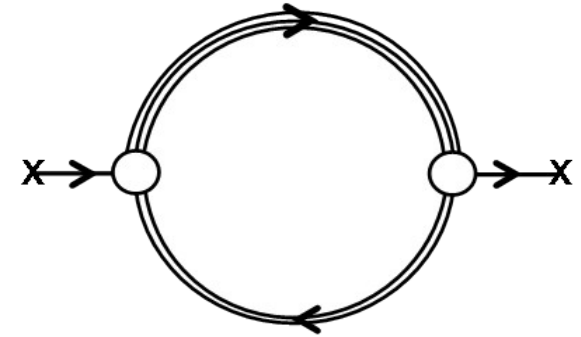
Φ -functional



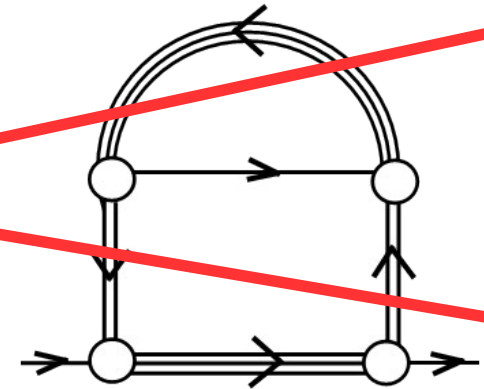
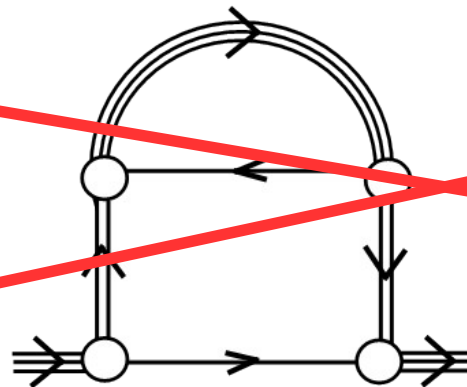
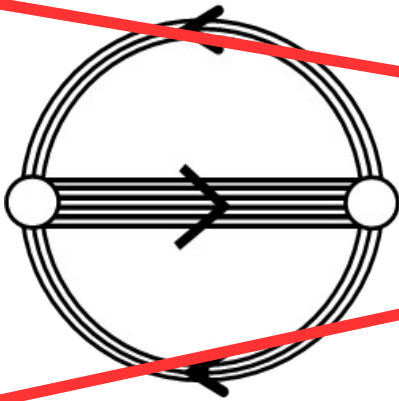
nucleon selfenergy



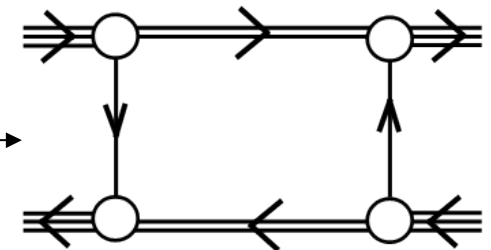
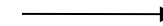
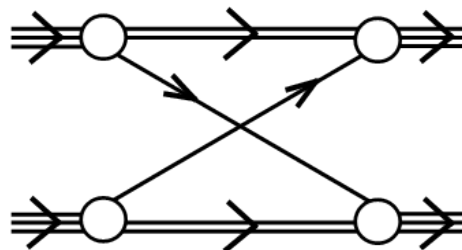
quark selfenergy



Not new! Already contained in above diagrams!

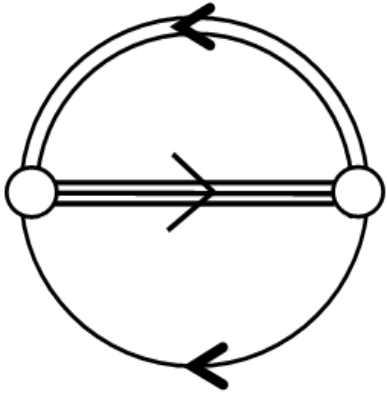


quark exchange interaction
between nucleons:

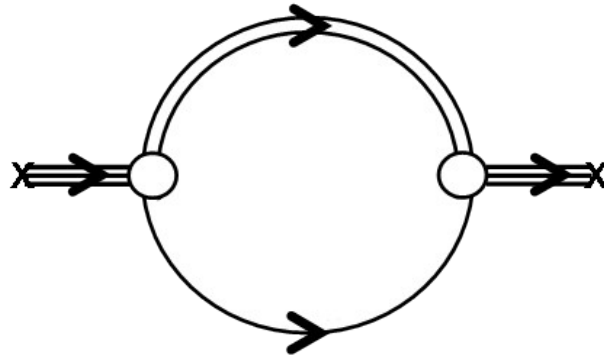


Example C: Nucleons in quark matter

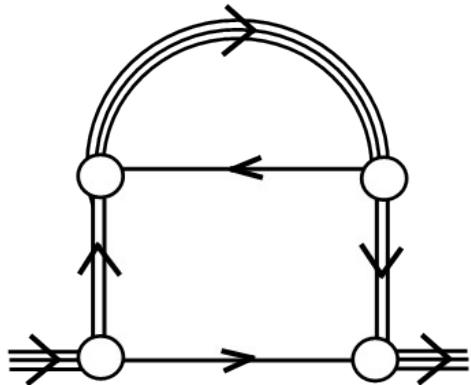
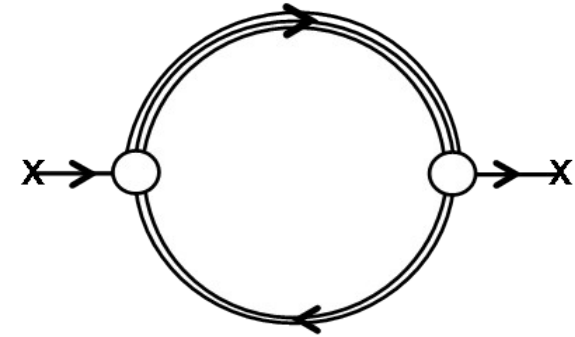
Φ -functional



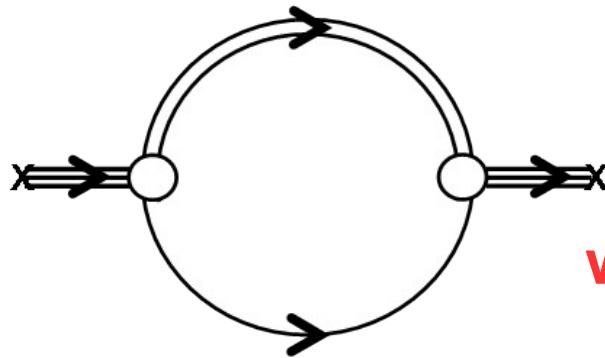
nucleon selfenergy



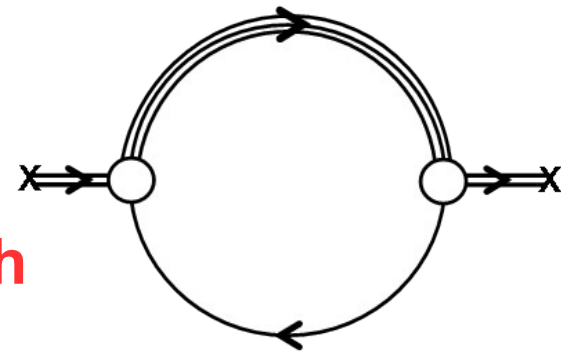
quark selfenergy



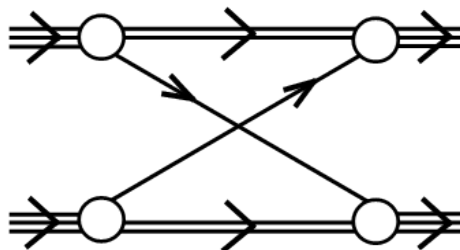
=



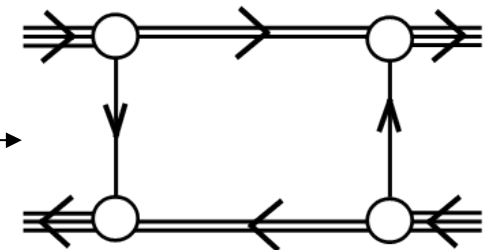
with



quark exchange interaction
between nucleons:



→



Intermezzo: Structure of the baryon?



12-Apostle
Church,
Kars

Intermezzo: Structure of the baryon?



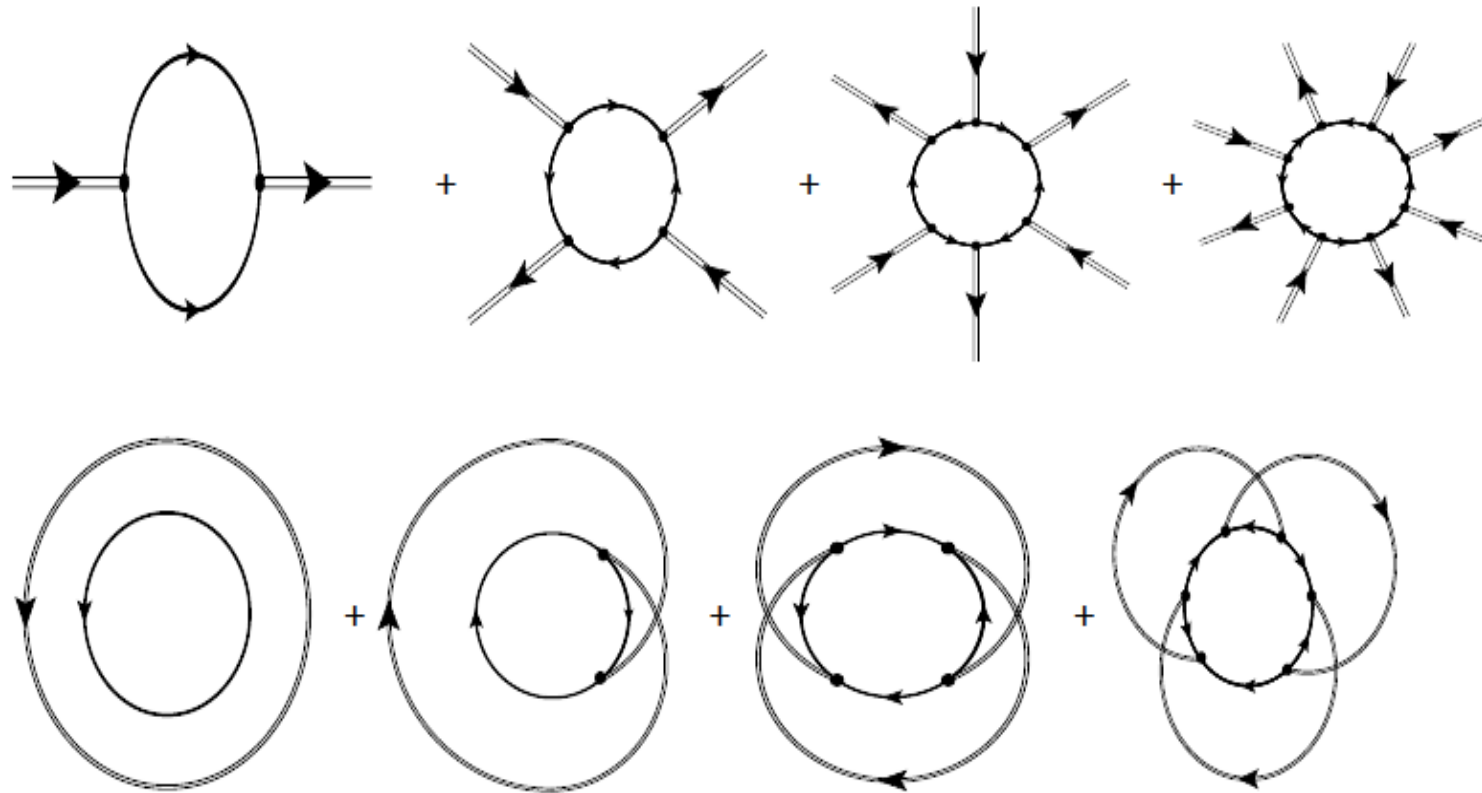
12-Apostle
Church,
Kars

Intermezzo: Structure of the baryon?

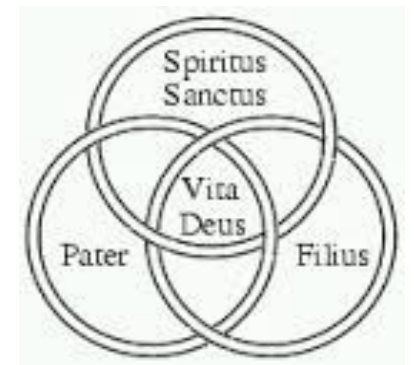
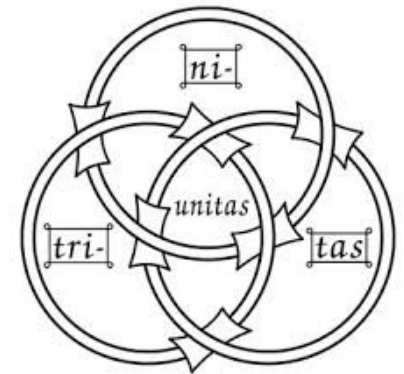
$$Z_{\text{fluct}} = \int D\Delta^\dagger D\Delta D\phi \exp\left\{-\frac{|\Delta|^2}{4G_D} - \frac{\phi^2}{4G} - \text{Tr} \ln S^{-1}[\Delta, \Delta^\dagger, \phi]\right\}$$

Cahill, Roberts, Prashifka: *Aust. J. Phys.* 42 (1989) 129, 161

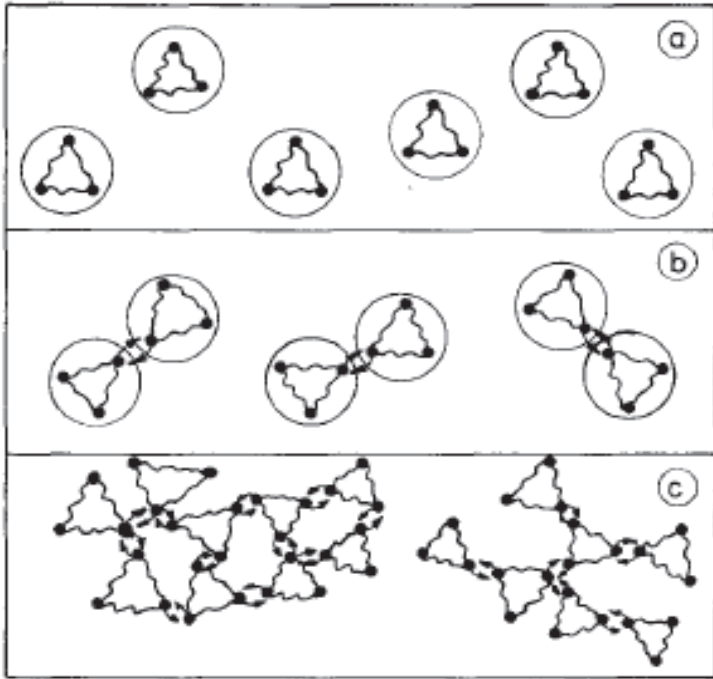
Cahill, *ibid*, 171; Reinhardt: *PLB* 244 (1990) 316; Buck, Alkofer, Reinhardt: *PLB* 286 (1992) 29



Borromean ? !!



Example C: Pauli blocking among baryons

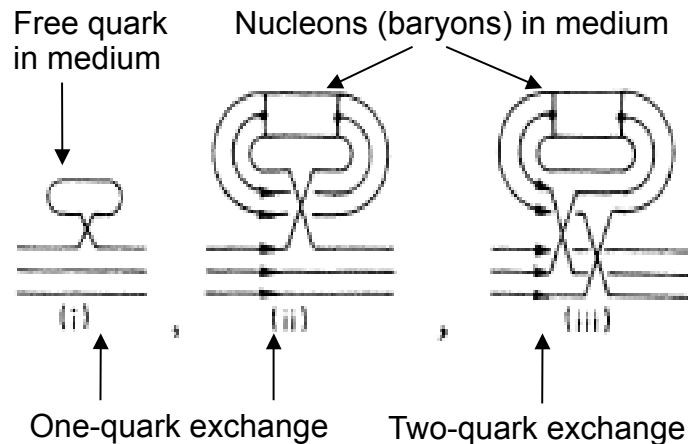


a) Low density: Fermi gas of nucleons (baryons)

b) ~ saturation: Quark exchange interaction and Pauli blocking among nucleons (baryons)

c) high density: Quark cluster matter (string-flip model ...)

Roepke & Schulz, Z. Phys. C 35, 379 (1987); Roepke, DB, Schulz, PRD 34, 3499 (1986)



Nucleon (baryon) self-energy --> Energy shift

$$\begin{aligned} \Delta E_{\nu P}^{\text{Pauli}} &= \sum_{123} |\psi_{\nu P}(123)|^2 [E(1) + E(2) + E(3) - E_{\nu P}^0] [f_{\alpha_1}(1) + f_{\alpha_2}(2) + f_{\alpha_3}(3)] \\ &+ \sum_{123} \sum_{456} \sum_{\nu P'} \psi_{\nu P}^*(123) \psi_{\nu P'}(456) f_3(E_{\nu P'}^0) \{ \delta_{36} \psi_{\nu P}(123) \psi_{\nu P'}^*(456) - \psi_{\nu P}(453) \psi_{\nu P'}^*(126) \} \\ &\quad \times [E(1) + E(2) + E(3) + E(4) + E(5) + E(6) - E_{\nu P}^0 - E_{\nu P'}^0] \\ &= \Delta E_{\nu P}^{\text{Pauli, free}} + \Delta E_{\nu P}^{\text{Pauli, bound}} \end{aligned}$$



PHYSICAL REVIEW D

VOLUME 34, NUMBER 11

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Pauli quenching effects in a simple string model of quark/nuclear matter

G. Röpke and D. Blaschke

Department of Physics, Wilhelm-Pieck-Universität, 2500 Rostock, German Democratic Republic

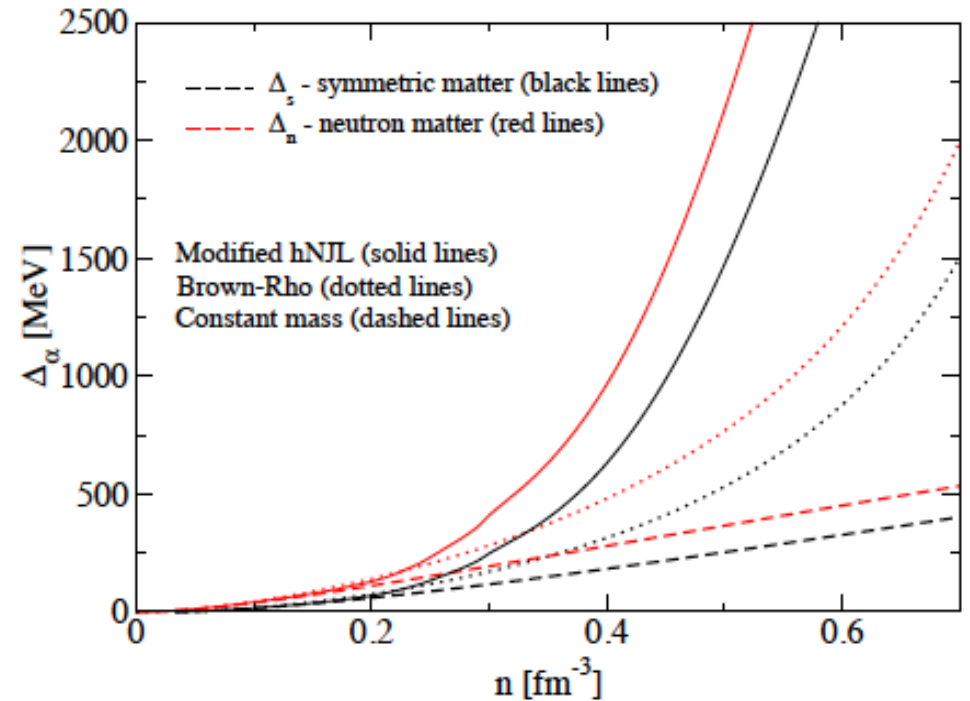
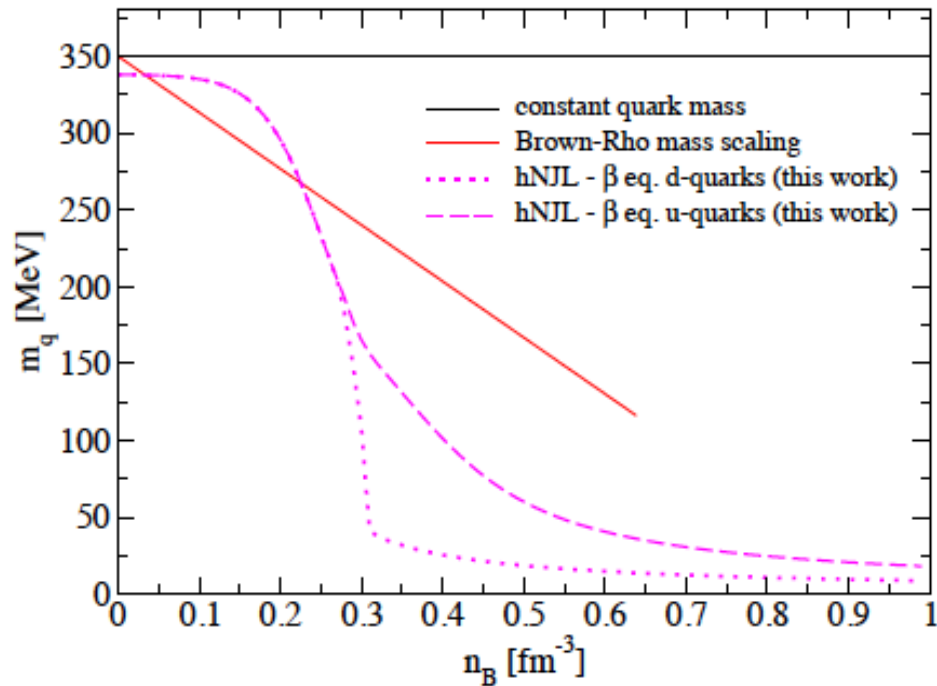
H. Schulz

*Central Institute for Nuclear Research, Rossendorf, 8051 Dresden, German Democratic Republic
and The Niels Bohr Institute, 2100 Copenhagen, Denmark*

(Received 16 December 1985)

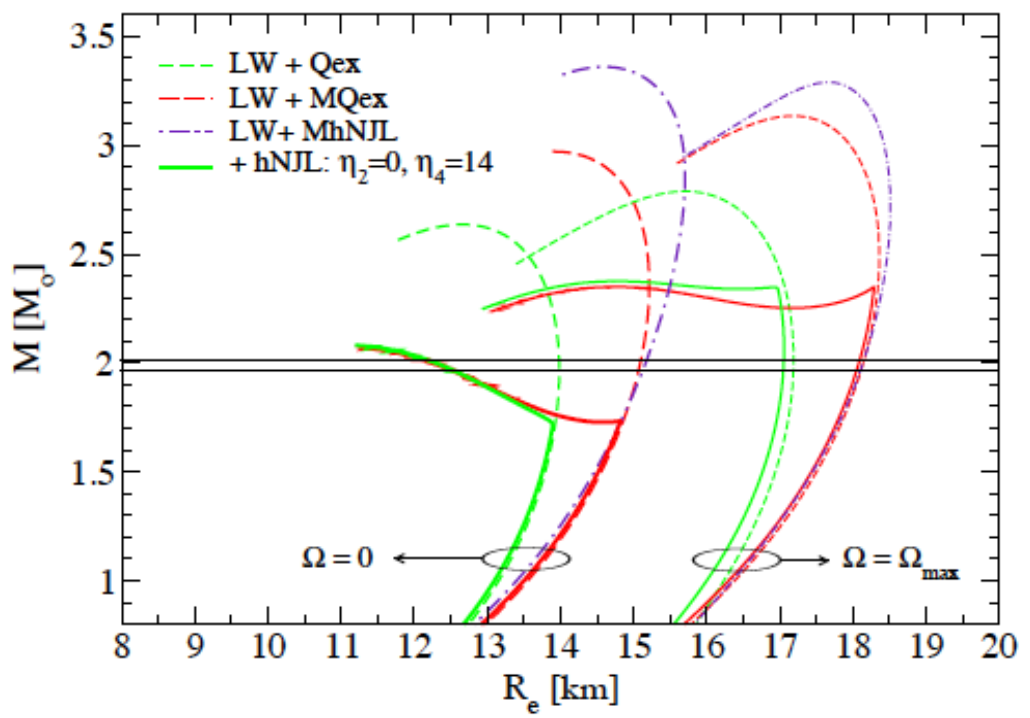
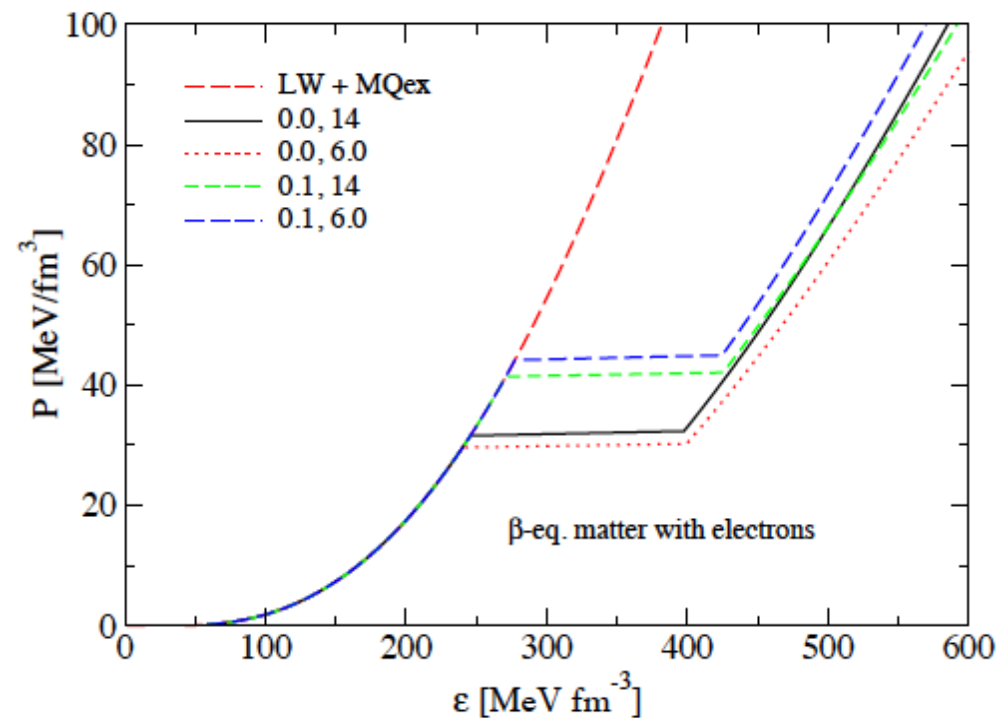
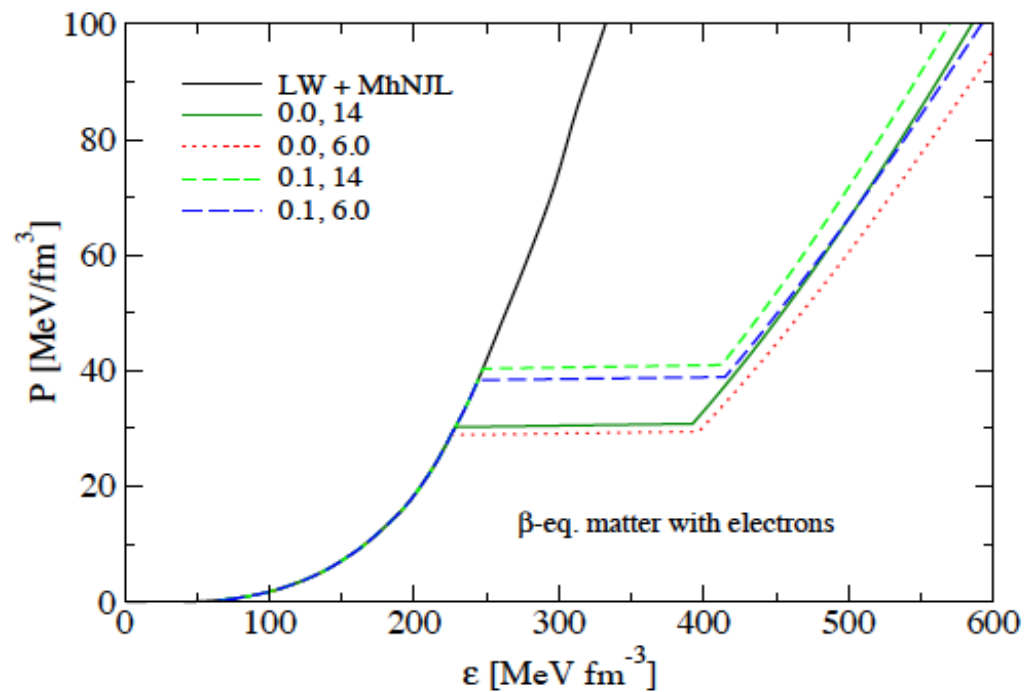
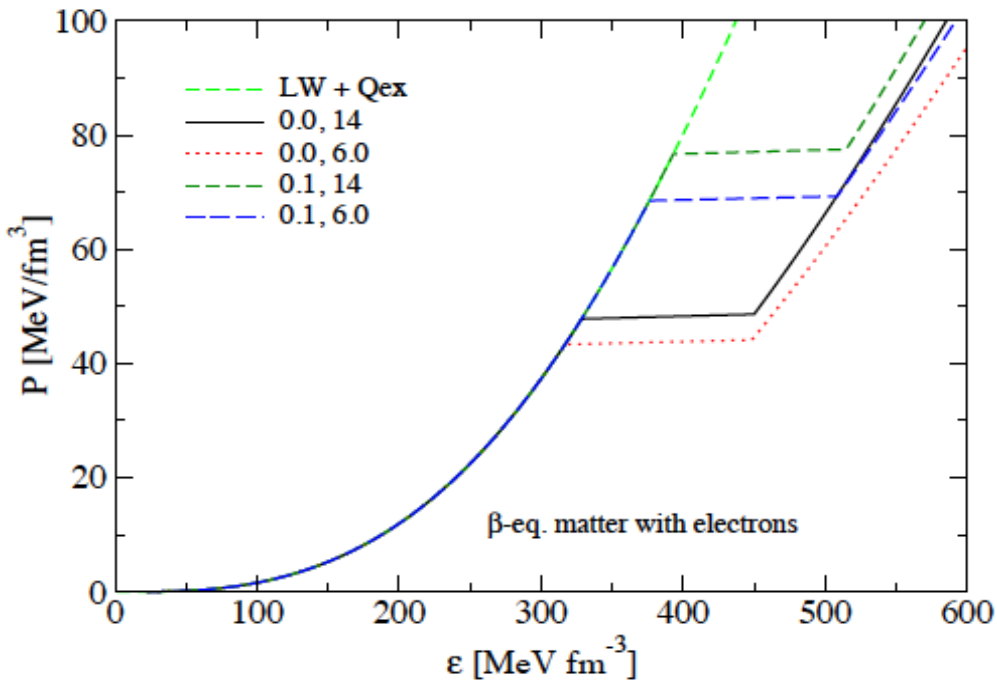
Example C: Pauli blocking in NM – details

New aspect: chiral restoration --> dropping quark mass



Increased baryon swelling at supersaturation densities:
--> dramatic enhancement of the Pauli repulsion !!

Example C: Pauli blocking in NM – results



Example C: Pauli blocking in NM – Summary

Pauli blocking selfenergy (cluster meanfield) calculable in potential models for baryon structure

Partial replacement of other short-range repulsion mechanisms (vector meson exchange)

Modern aspects:

- onset of chiral symmetry restoration enhances nucleon swelling and Pauli blocking at high n
- quark exchange among baryons \rightarrow six-quark wavefunction \rightarrow “bag melting” \rightarrow deconfinement

Chiral stiffening of nuclear matter \rightarrow reduces onset density for deconfinement

Hybrid EoS:

Convenient generalization of RMF models,

Take care: eventually aspects of quark exchange already in density dependent vertices!

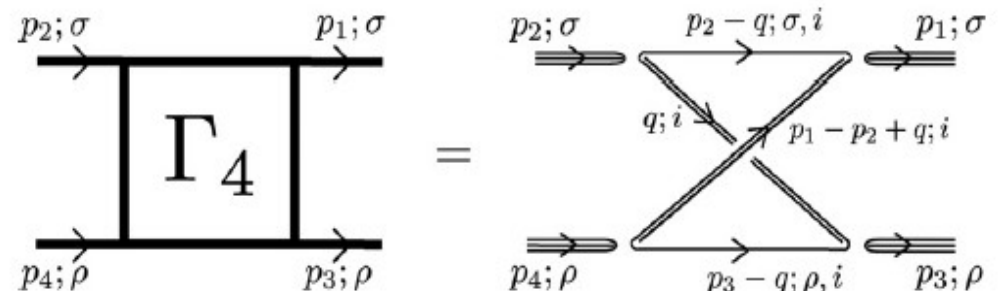
Other baryons:

- hyperons
- deltas

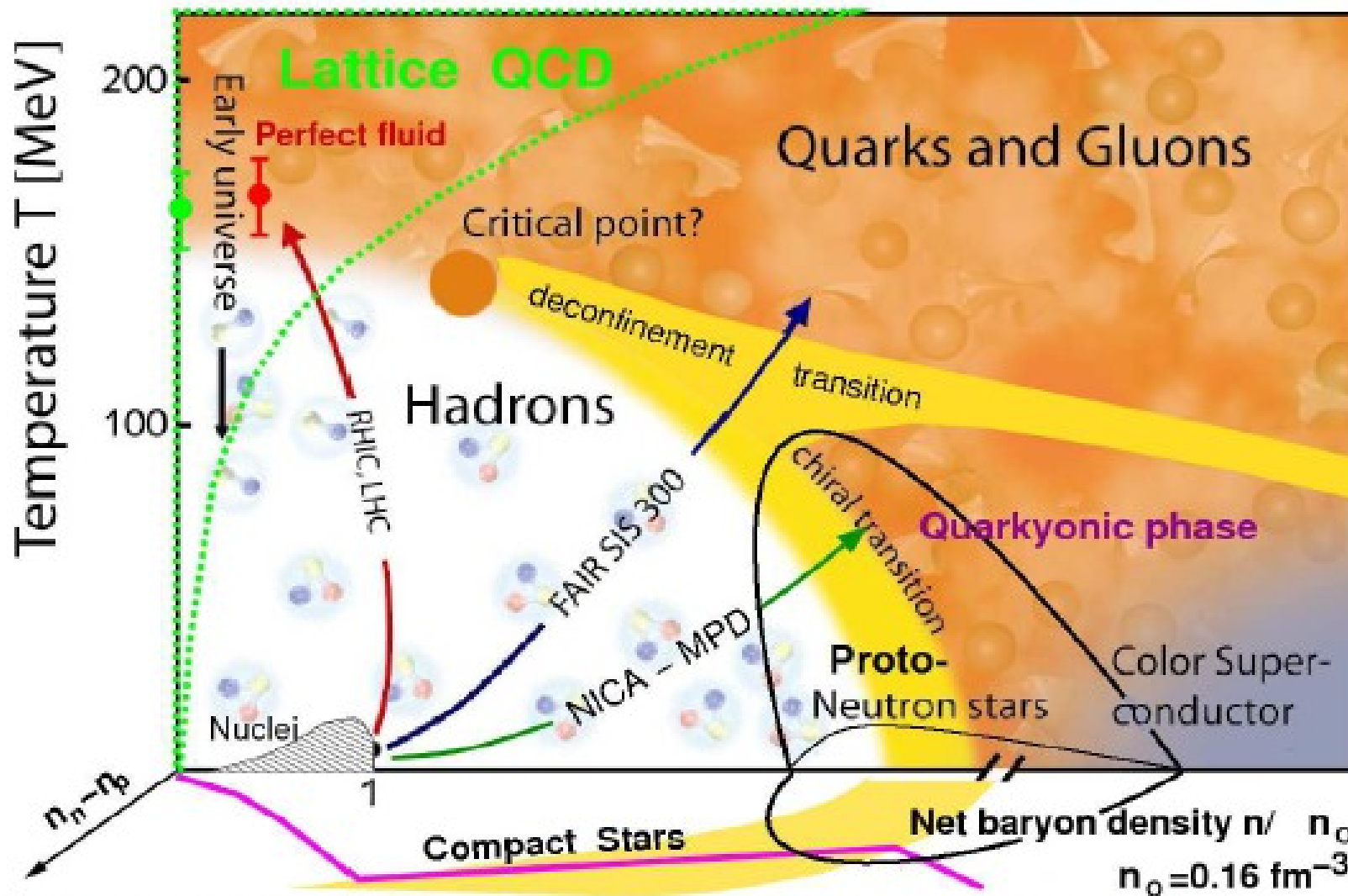
Again calculable, partially done in nonrelativistic quark exchange models, chiral effects not yet!

Relativistic generalization:

Box diagrams of quark-diquark model ...



Support a CEP in QCD phase diagram with Astrophysics?



NICA White Paper, <http://theor.jinr.ru/twiki-cgi/view/NICA/WebHome>

S. Benic et al., A&A 577, A40 (2015)

Crossover at finite T (Lattice QCD) + First order at zero T (Astrophysics) = Critical endpoint exists!